

# Effects from QCD **color** flow in proton-proton and proton-nucleus collisions

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Joe Osborn

University of Michigan

September 14, 2018



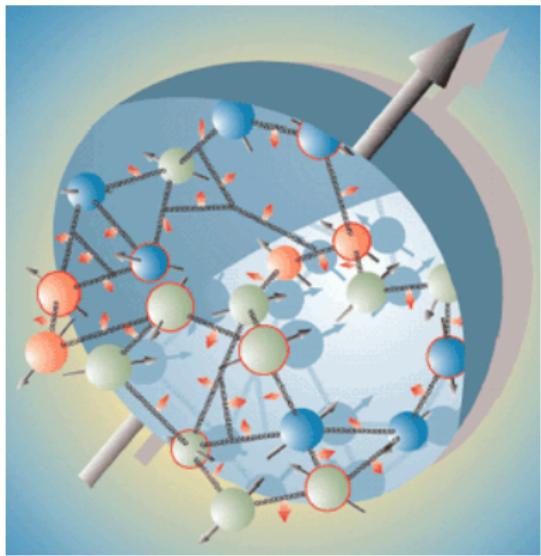
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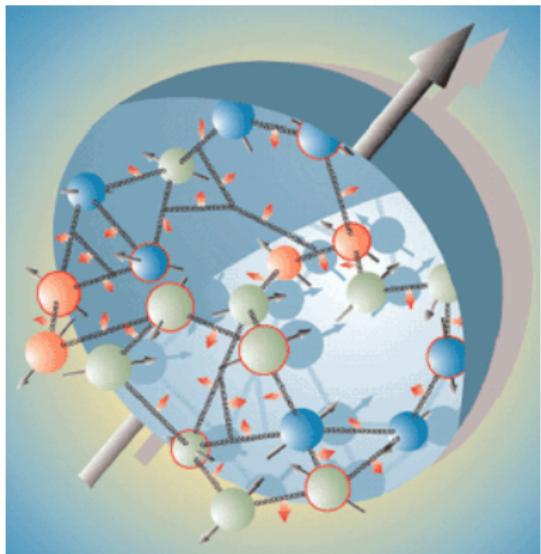
# Quantum Chromodynamics

- QCD is the fundamental gauge theory describing the strong force
- Written in terms of quark and gluon (parton) degrees of freedom



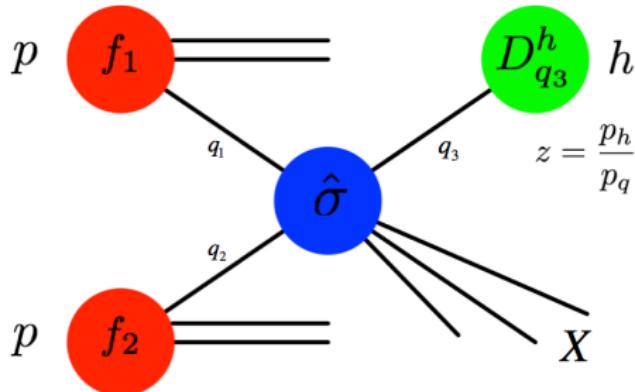
# Quantum Chromodynamics

- QCD is the fundamental gauge theory describing the strong force
- Written in terms of quark and gluon (parton) degrees of freedom
- But we can only directly observe combinations of partons in the laboratory!
- Confinement and the non-Abelian nature of QCD: gluon self coupling and **color** charge



# QCD Cross Sections

- To account for bound state nature of hadrons, cross sections are factorized
- Nonperturbative parton distribution and fragmentation functions (PDFs and FFs) are used to describe the individual partons within a hadron

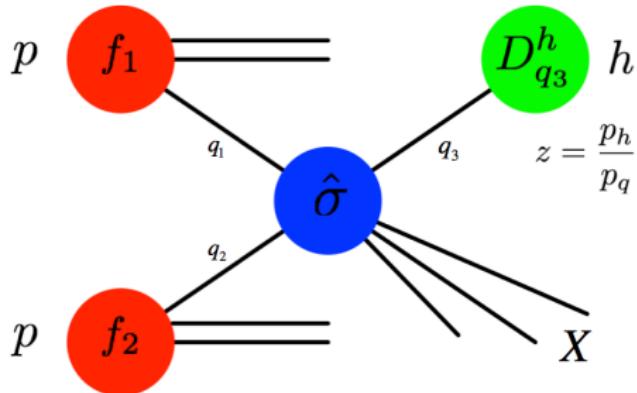


$$\sigma = f_1(x, Q^2) \otimes f_2(x, Q^2) \otimes \frac{d\hat{\sigma}}{dt} \otimes D_q^h(z, Q^2)$$

$$x = \frac{p_{parton}}{p_{proton}}$$

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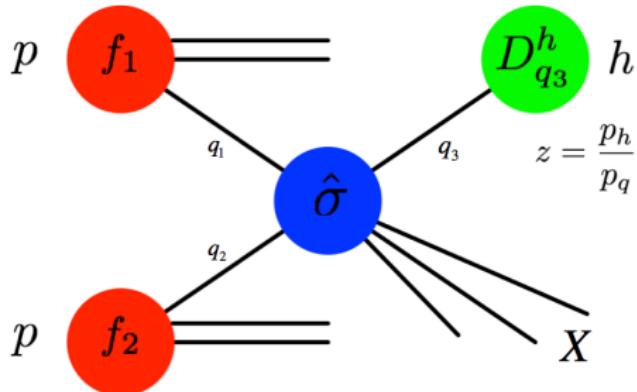


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- Taken to be process independent and uncorrelated

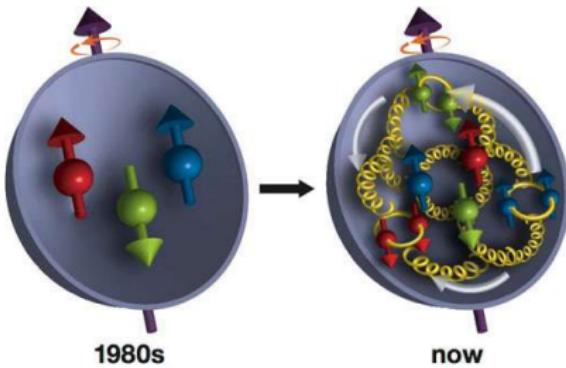


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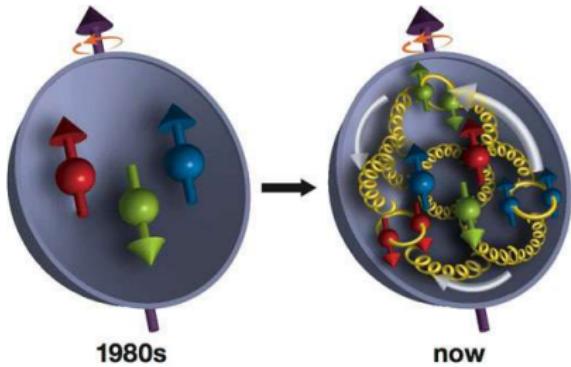
# The Proton Multidimensionally

- Historically, the structure of the proton has been approximated as only dependent on the collinear momentum fraction  $x$
- The last two decades have seen QCD move from a static to dynamic picture of the proton



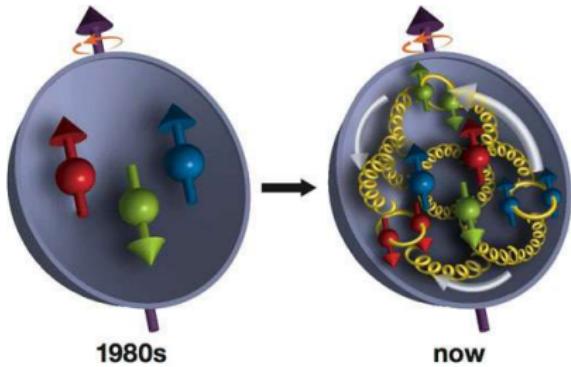
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  - Position (2D)
  - Spin
  - Flavor
  - Momentum (3D)
  - Color (!)

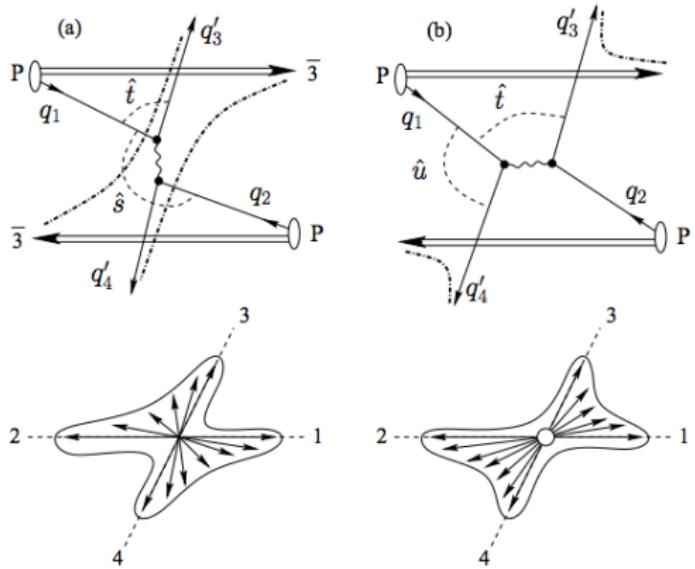


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- 
- The diagram shows two circular cross-sections of a proton, separated by a horizontal arrow pointing from left to right, representing the progression of time. The left circle, labeled '1980s', contains three quarks (red, blue, green) with arrows indicating their spins, and a small purple quark at the top. The right circle, labeled 'now', contains the same three quarks, but they are surrounded by a dense, swirling network of yellow gluons, representing the dynamic, non-perturbative state of the proton's interior.
- Momentum (3D)
  - Color (!)

# Color Coherence

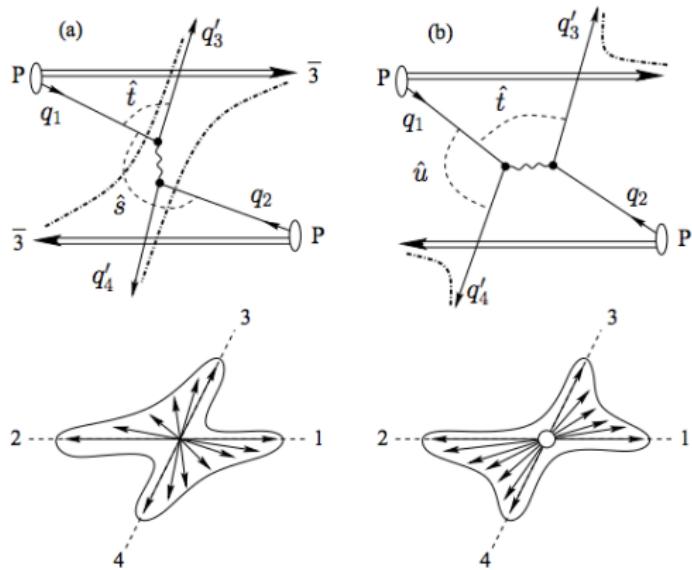
- Color flow through hard processes leads to certain regions of particle production in hadronic collisions



Y. Dokshitzer. Basics of Perturbative QCD, 1991

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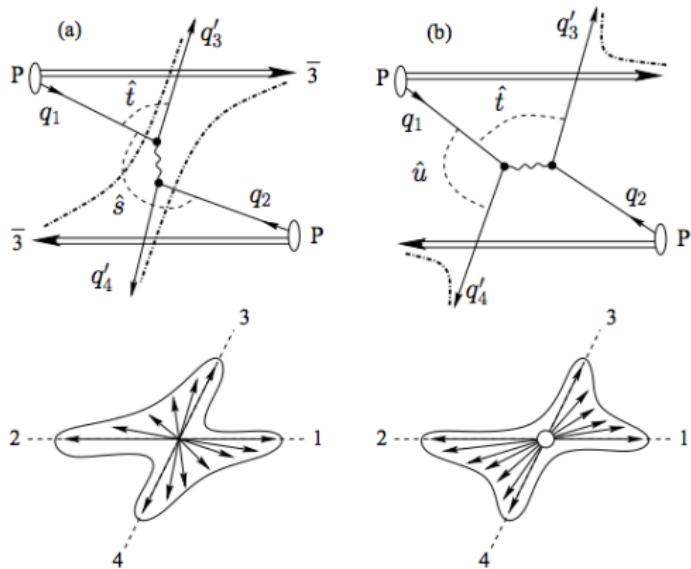
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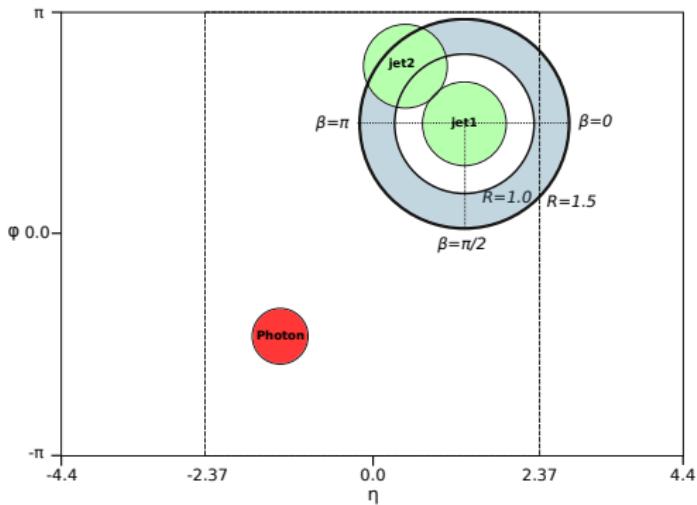
- Color flow through hard processes leads to certain regions of particle production in hadronic collisions
- Color connects hard scattered partons with remnants of other proton
- Color connections lead to destructive gluon interferences  
→ depletions in hadron production



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# Color Coherence Measurements

Nucl. Phys. B 918, 257 (2017)



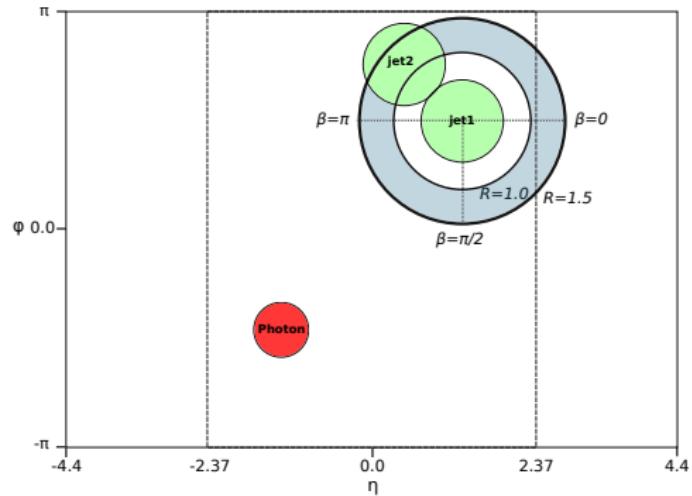
- Color coherence measurements study:

$$\beta = \tan^{-1} \frac{\Delta\phi_{21}}{\text{sign}(\eta_1)\Delta\eta_{21}}$$

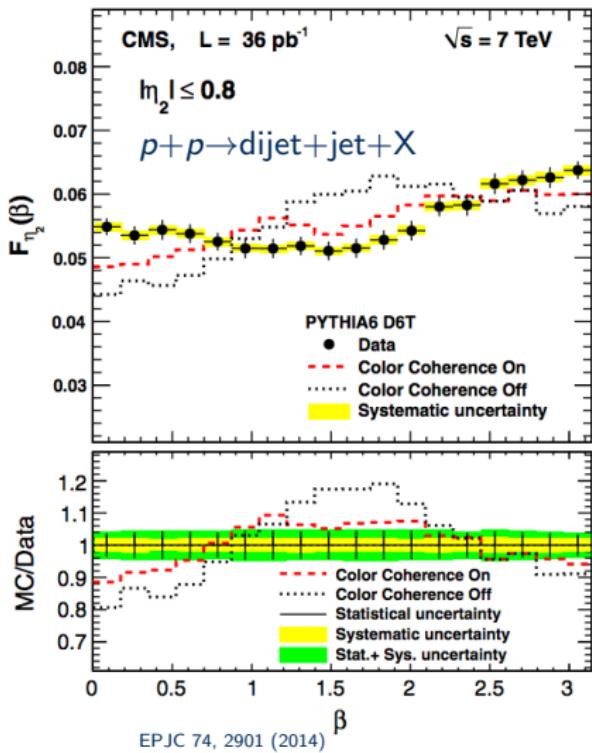
- Angle in  $(\eta, \phi)$  space between sub-leading hard-scattered jet and gluon initiated jet
- $\beta = 0$  points to the beam closer to jet 1 in  $(\eta, \phi)$  space
- $\beta = \pi$  points to the beam farther from jet 1 in  $(\eta, \phi)$  space

# Color Coherence Measurements

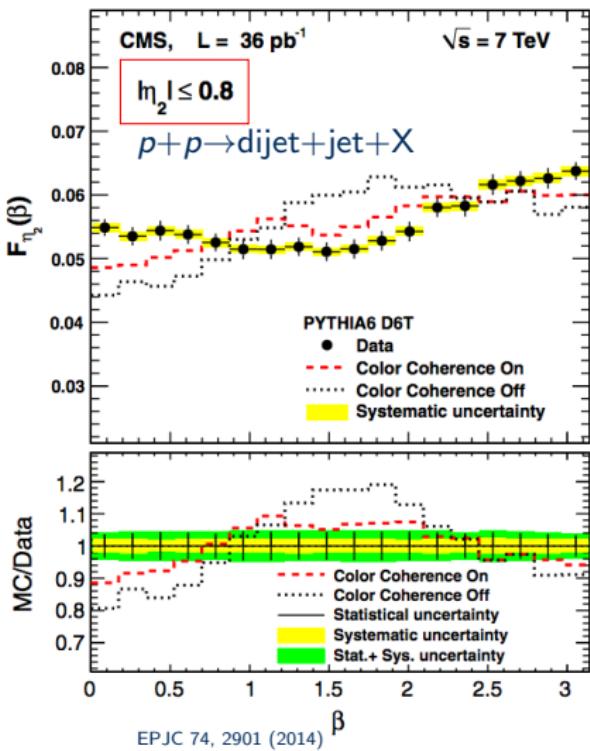
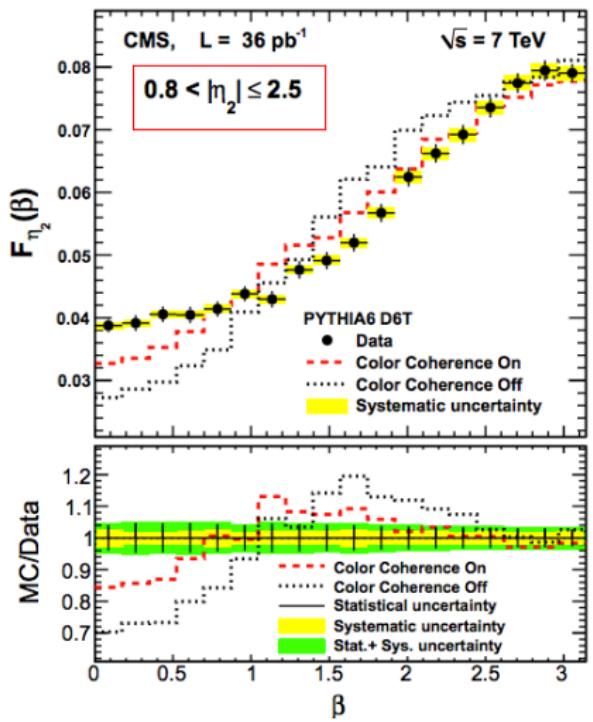
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- Third jet more likely to be found at  $\beta = 0, \beta = \pi$ , i.e. similar  $\phi$  but large  $\eta$  gap (remnant activity high!)



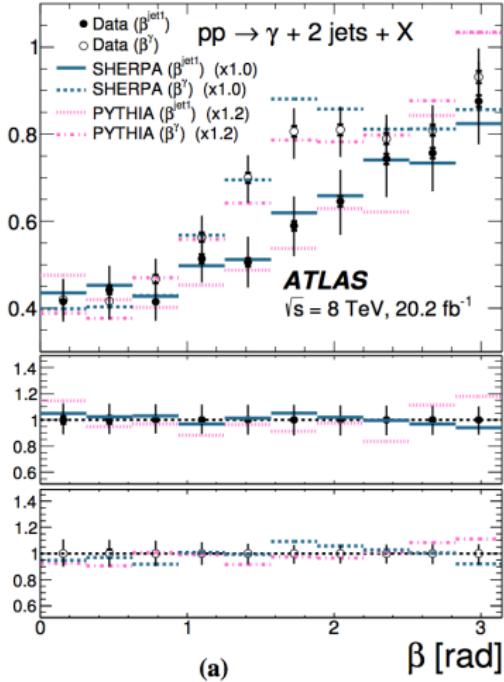
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- Even stronger correlation to opposite beam at forward rapidities!

# Color Coherence Measurements

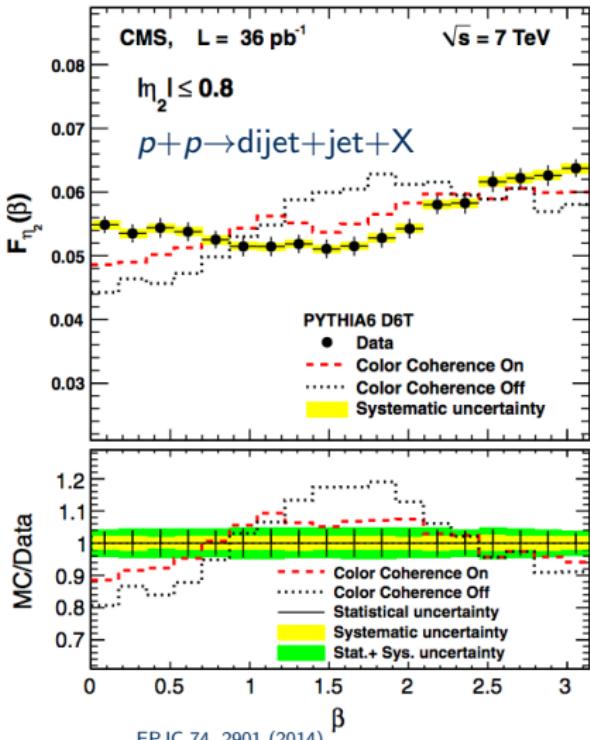
$d\sigma/d\beta$  [pb]



(a)

Nucl. Phys. B 918, 257 (2017)

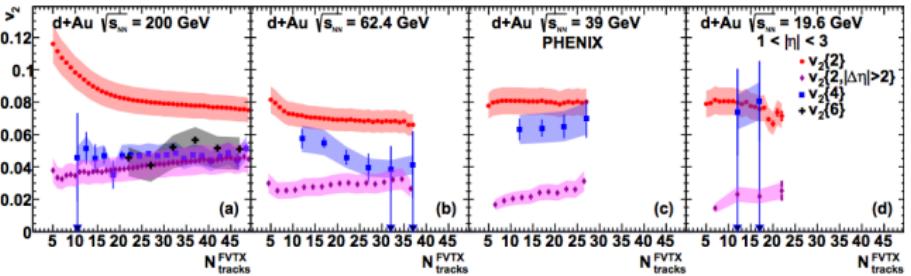
- Even stronger correlation to opposite beam when using  $\gamma$ -jet!



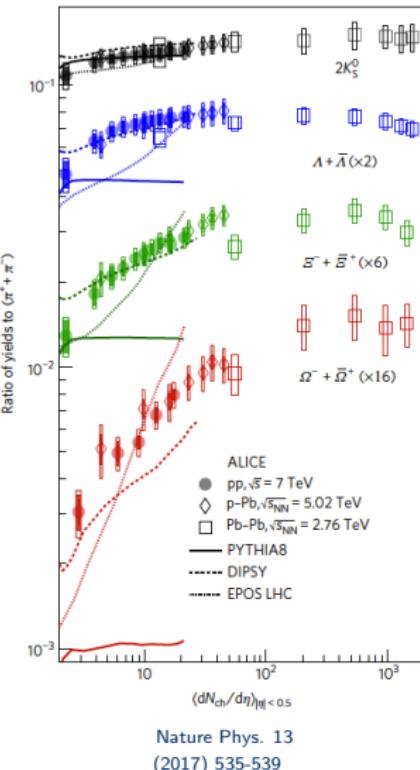
EPJC 74, 2901 (2014)

# Relation to High Multiplicity?

- Surprising results from RHIC and LHC show novel phenomena in high multiplicity  $p+p$  and  $p+A$
- What role does color play in these measurements?
- Color coherence measurements also probing (parton) long range  $\eta$  correlations

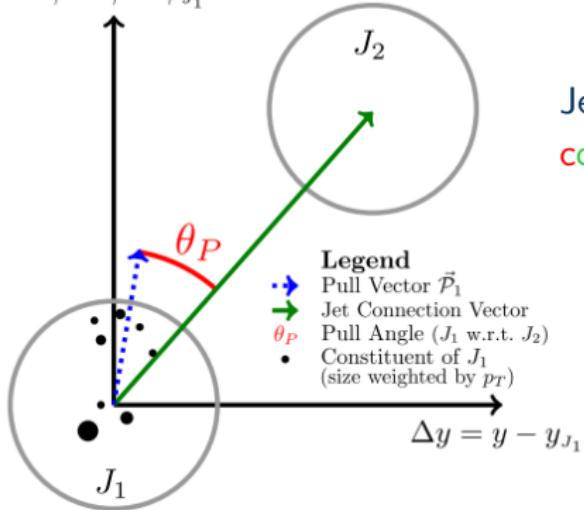


PRL 120, 062302 (2018)



# Jet Substructure

$$\Delta\phi = \phi - \phi_{J_1}$$

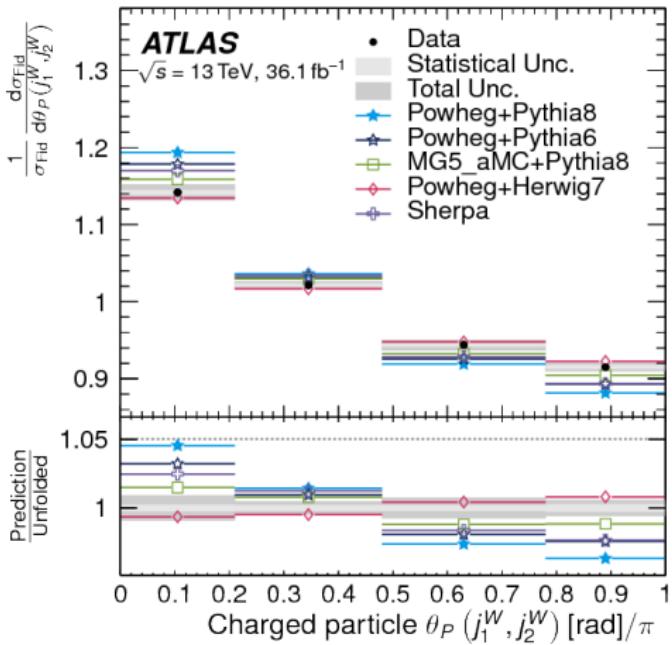
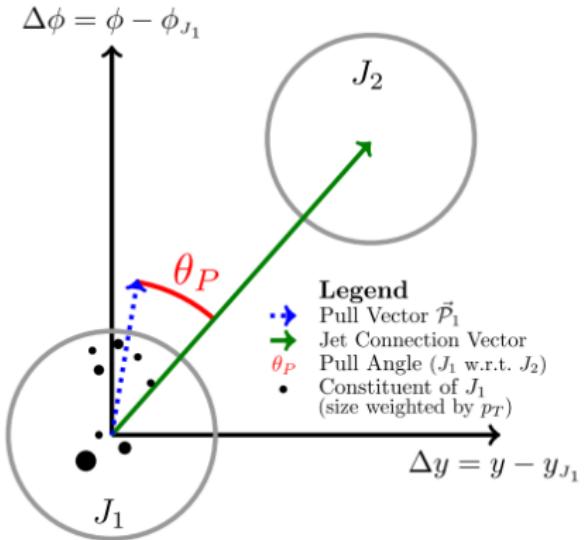


Jet-pull vector predicted to be sensitive to  
color connections (PRL 105, 022001 (2010))

$$\vec{\mathcal{P}}(j) = \sum_{i \in j} \frac{|\vec{\Delta r}_i| \cdot p_T^i}{p_T^j} \vec{\Delta r}_i$$

- Absence of color connection -  $\theta_p$  expected to be distributed uniformly
- Color connection -  $\theta_p$  expected to preferentially lie along jet connection vector  $\theta_p \sim 0$

# Jet Substructure



- Jet pull angle preferentially  $\sim 0 \rightarrow$  color connections
- Color affects radiation patterns within jets

arXiv:1805.02935

**Multidifferential observables are revealing the  
effects of color flow in  $p+p$  collisions**

## 1D vs. 3D Nonperturbative Functions

- There must be transverse structure due to the confined nature of the partons and the additional possibility of gluon radiation
- The unintegrated  $k_T$  distributions are explicitly dependent on transverse momentum

Parton Distribution Functions:  $f(x) \rightarrow f(x, k_T)$

Fragmentation Functions:  $D(z) \rightarrow D(z, j_T)$

$$\sigma = f_{q/h}(x, k_T, Q^2) \otimes \frac{d\hat{\sigma}}{dt} \otimes D_{q/h}(z, j_t, Q^2)$$

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$$\implies \Lambda_{QCD} \lesssim k_T \ll Q$$

$\implies$  Multi-scale observables necessary!

# Transverse-Momentum-Dependent Phenomenology

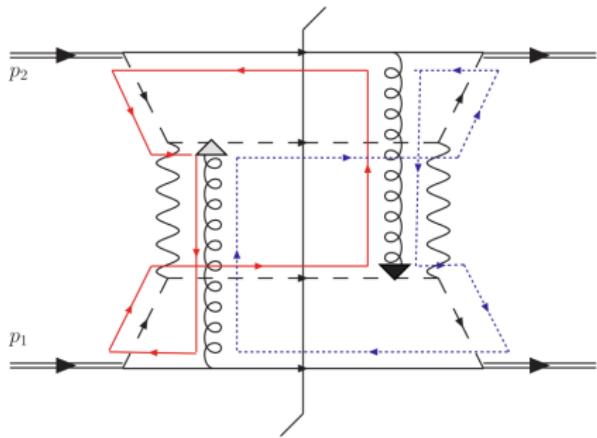
- In the collinear framework, nonperturbative functions are taken to be uncorrelated, universal, process independent functions
- In the transverse-momentum-dependent framework, it has been necessary to re-check these assumptions

# Transverse-Momentum-Dependent Phenomenology

- In the collinear framework, nonperturbative functions are taken to be uncorrelated, universal, process independent functions
- In the transverse-momentum-dependent framework, it has been necessary to re-check these assumptions
- What happens in leading-order QCD processes where a **colored** quark or gluon is exchanged at the hard interaction vertex?
- **Color** present in both the initial and final state - therefore soft gluon exchange possible in both the initial and final state

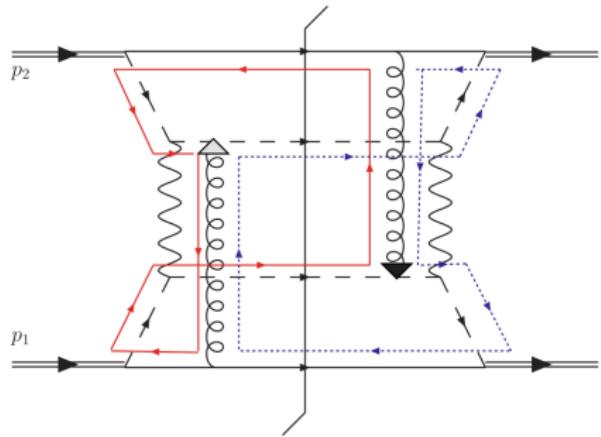
# Factorization Breaking of TMD Functions

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- TMD nonperturbative functions no longer defined - partons are quantum mechanically correlated via color across colliding hadrons!



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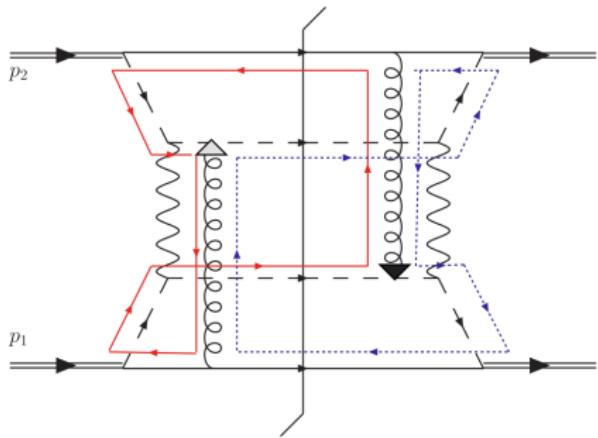
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↓

$$\sigma \stackrel{?}{=} CF(x_1, x_2, k_{T_1}, k_{T_2}, z_1, z_2, j_{T_1}, j_{T_2}) \otimes \frac{d\hat{\sigma}}{dt}$$

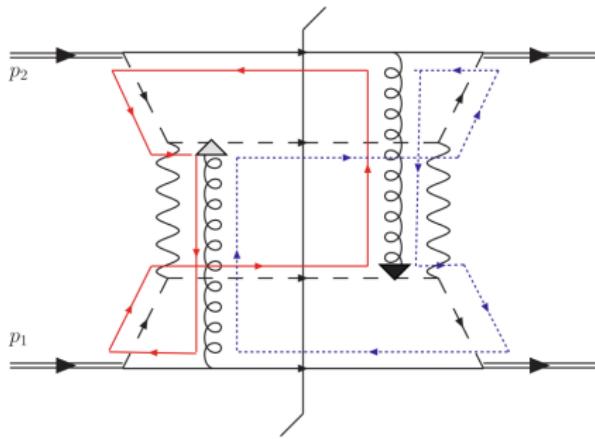
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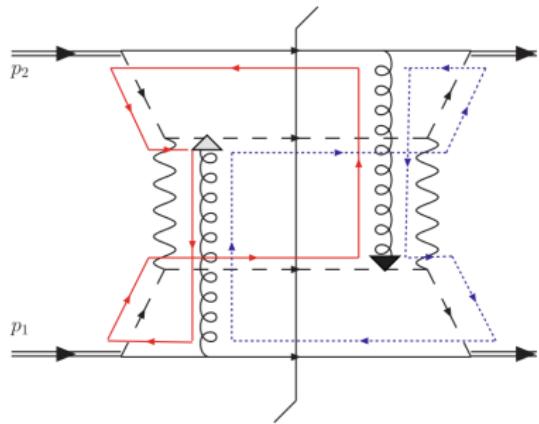
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- Consequence of QCD as a non-Abelian gauge theory

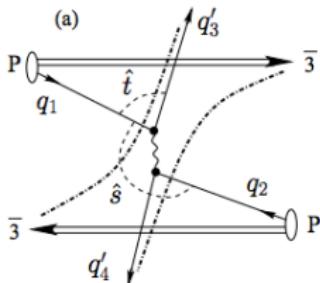
# Color Entanglement and Color Coherence

## Color entanglement



PRD 81, 094006 (2010)

## Color coherence



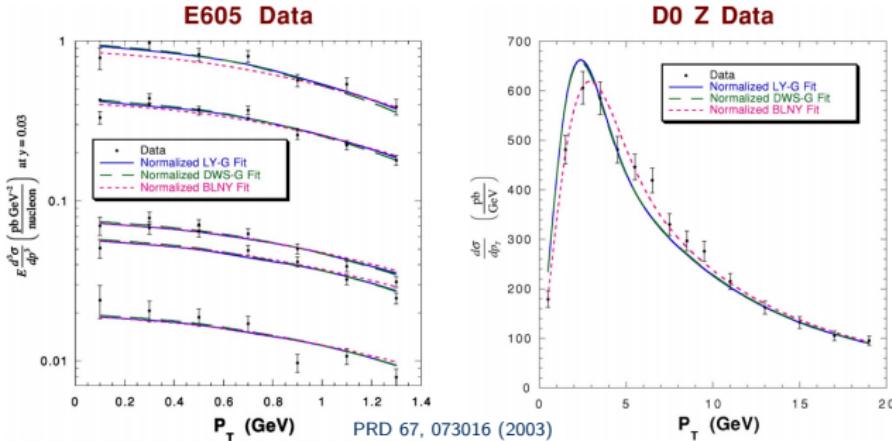
Y. Dokshitzer. Basics of Perturbative QCD, 1991

- The same underlying QCD phenomena at play - color leads to nonperturbative consequences

How can we search for effects from TMD  
color entanglement?

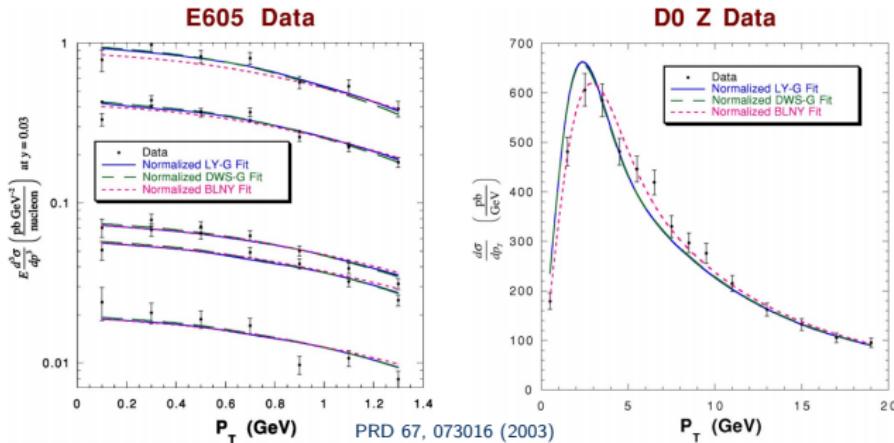
# Collins-Soper-Sterman (CSS) Evolution with $Q^2$

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- Has been used to successfully describe global Drell-Yan and Tevatron  $Z^0$  cross sections



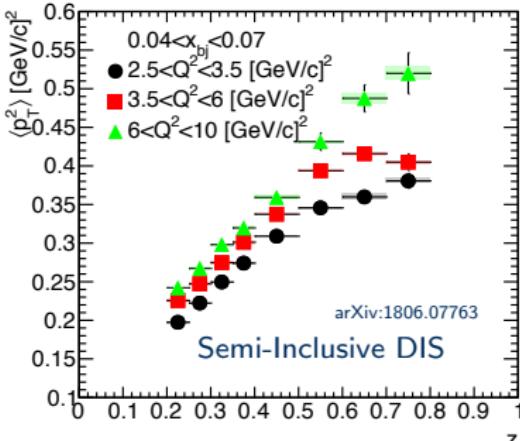
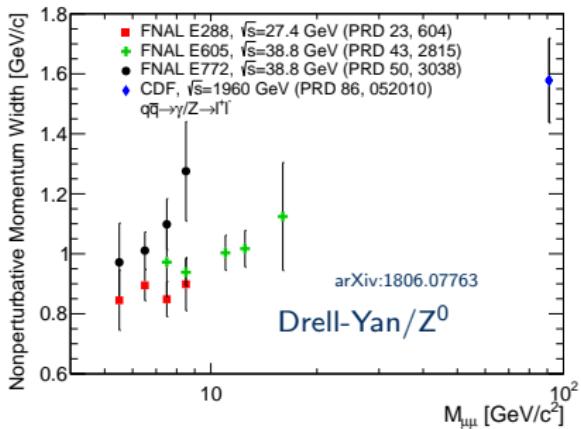
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- Clear qualitative prediction - momentum widths sensitive to nonperturbative transverse momentum increase with increasing hard scale
- Due to increased phase space for gluon radiation



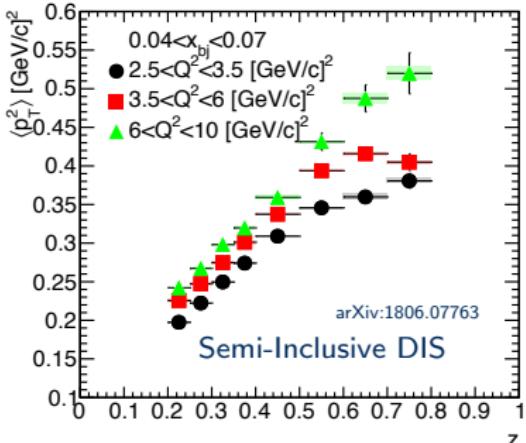
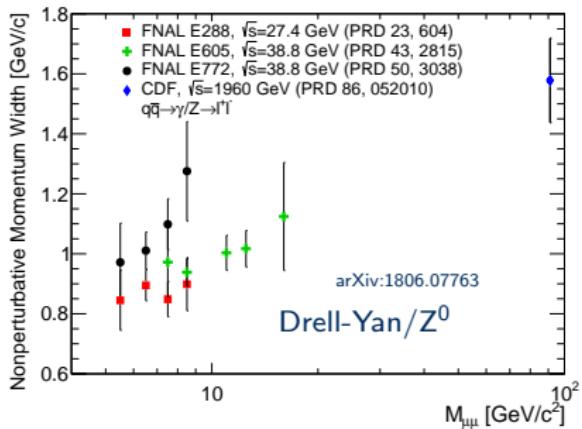
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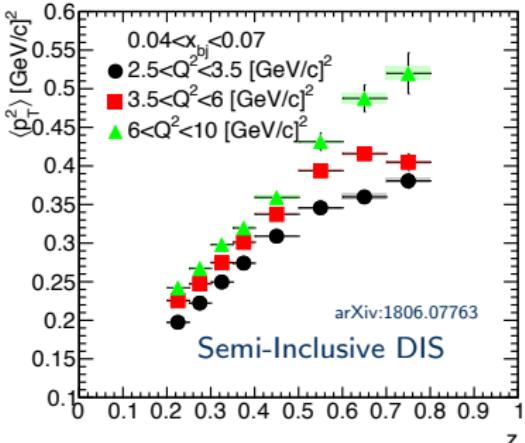
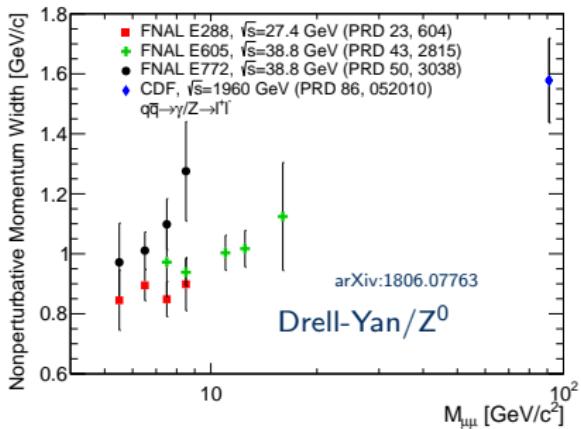
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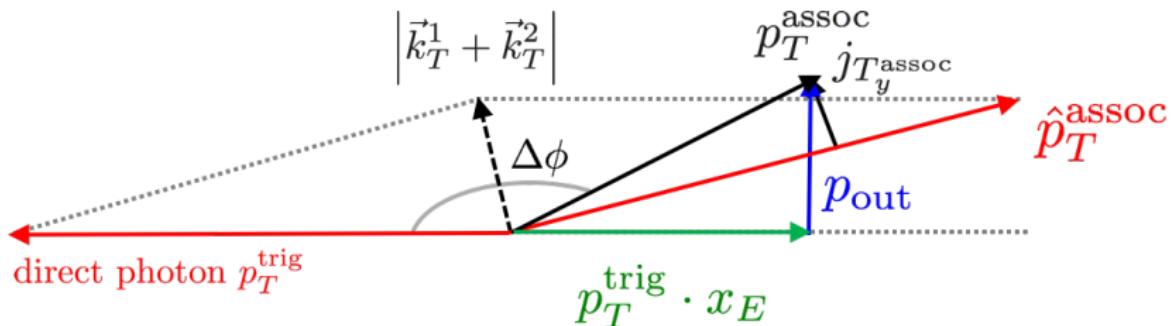


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  - If TMD factorization, then CSS evolution. If not CSS evolution, then not TMD factorization!

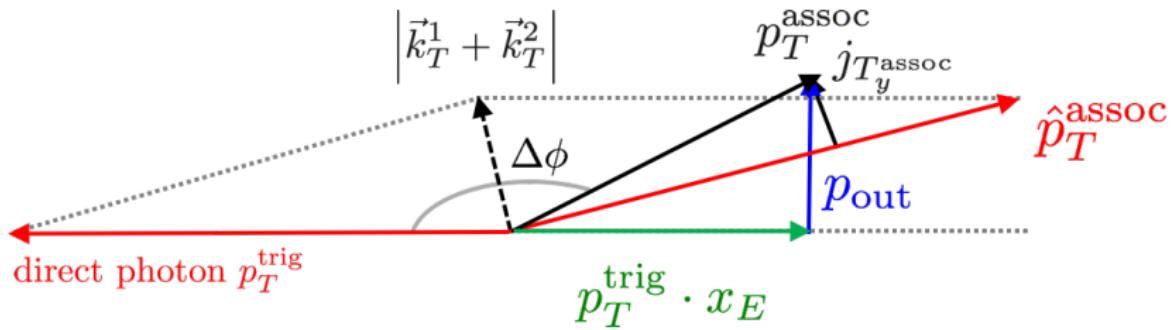


## Observables To Probe Entanglement



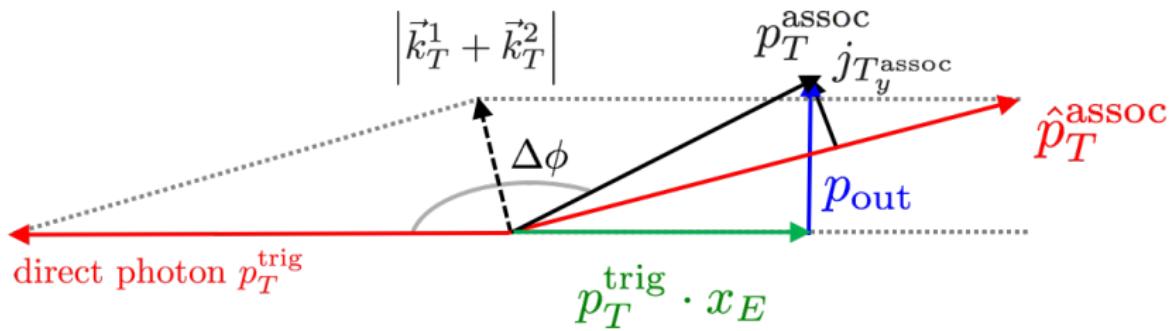
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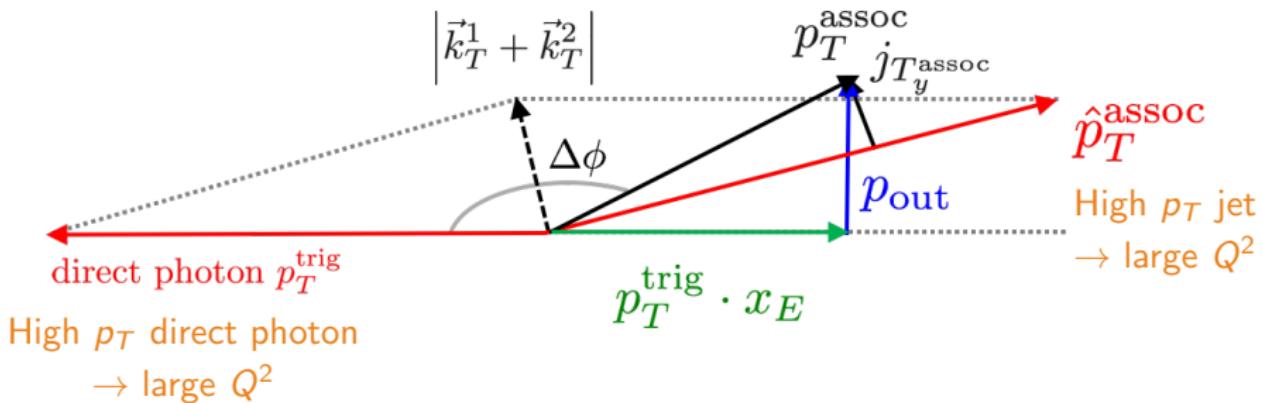
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  - Can use  $p + p \rightarrow \gamma + h^\pm + X$  or  $p + p \rightarrow h^\pm + h^\pm + X$

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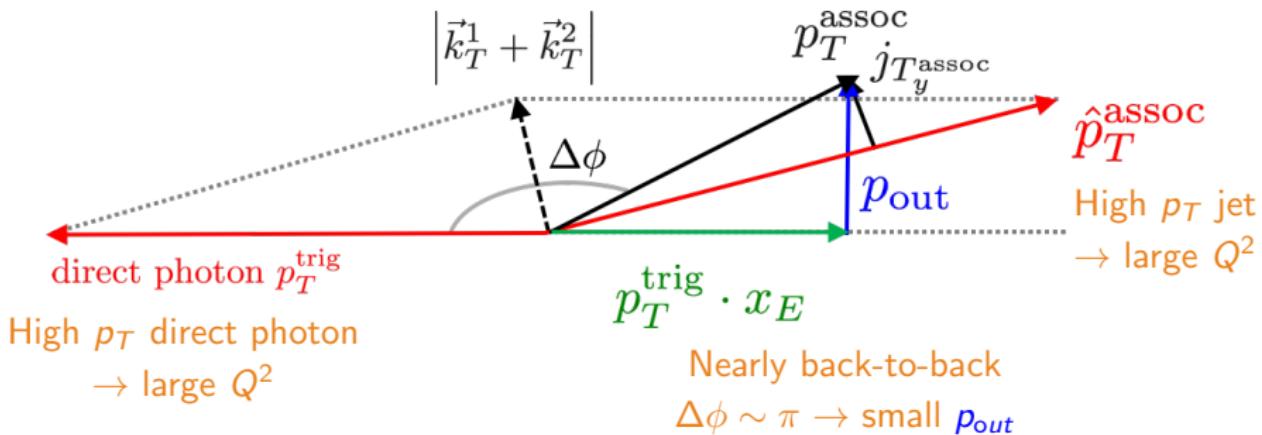
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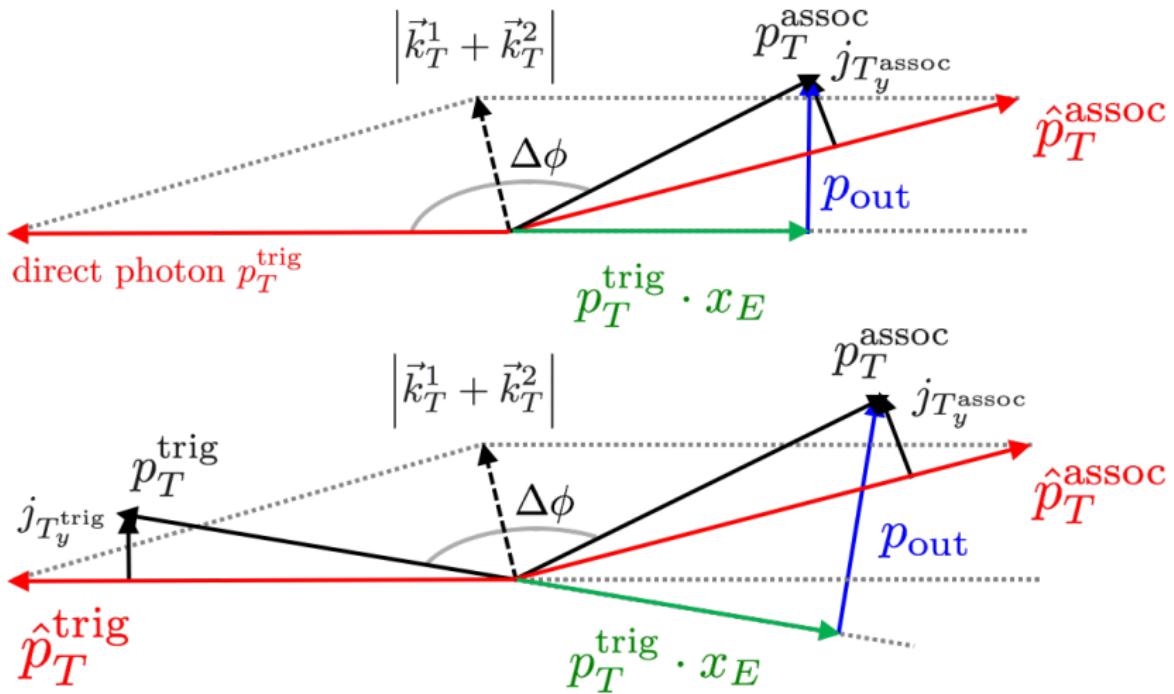
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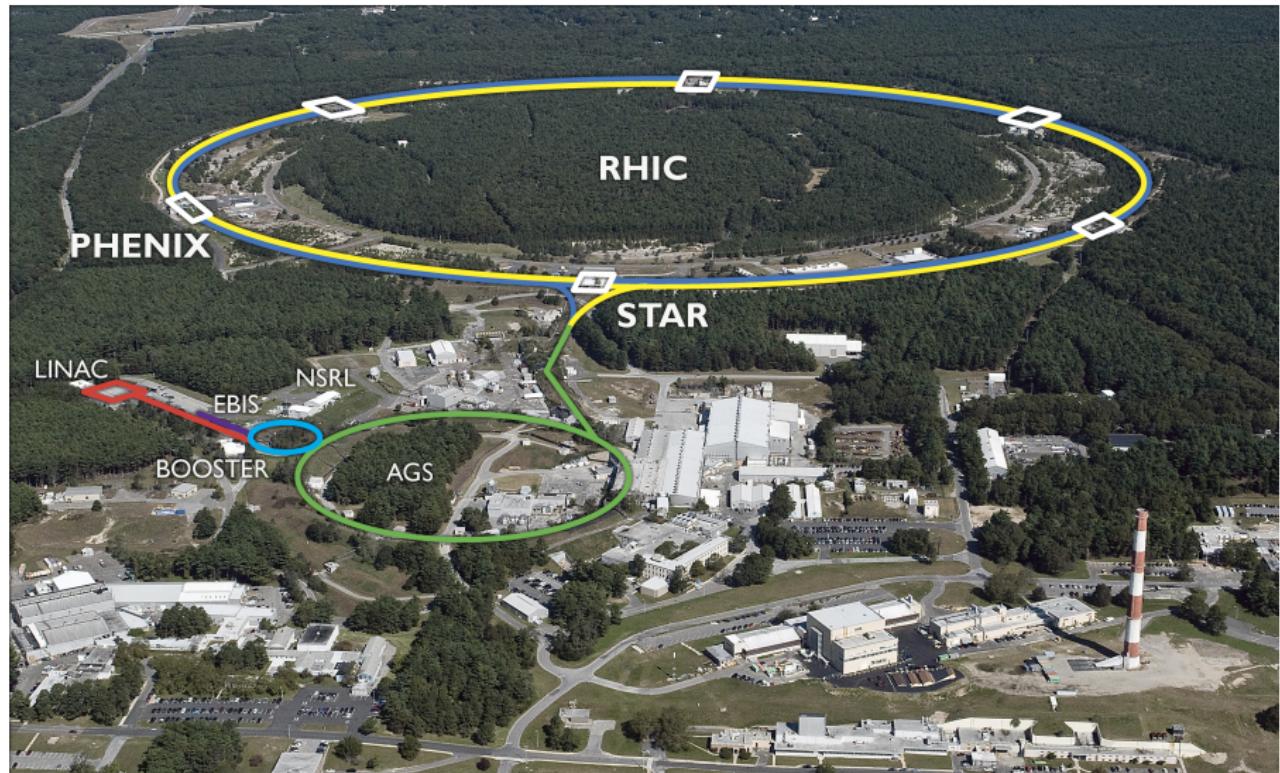


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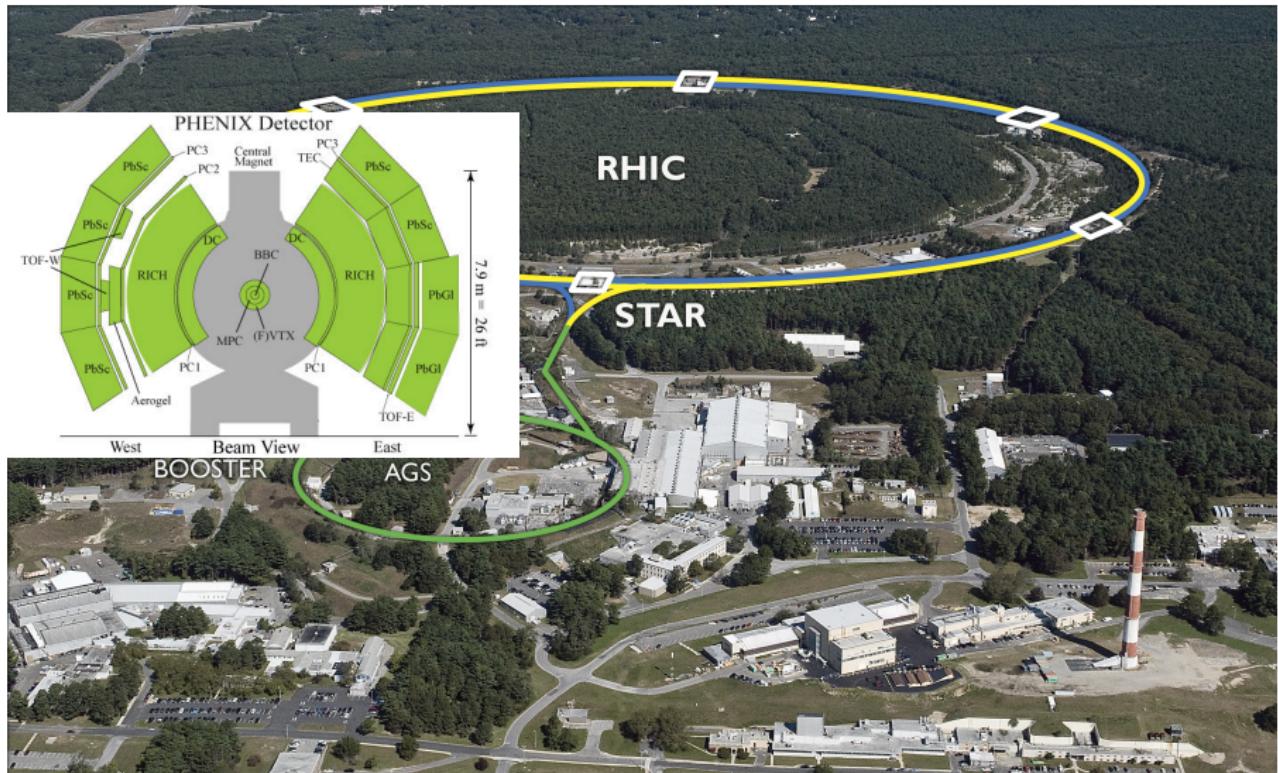
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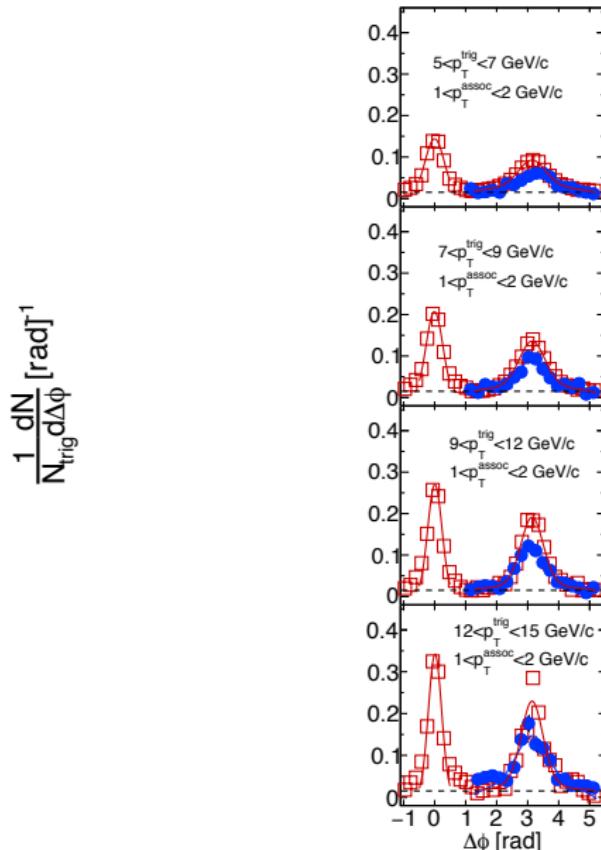
# Relativistic Heavy Ion Collider - RHIC at Brookhaven National Laboratory



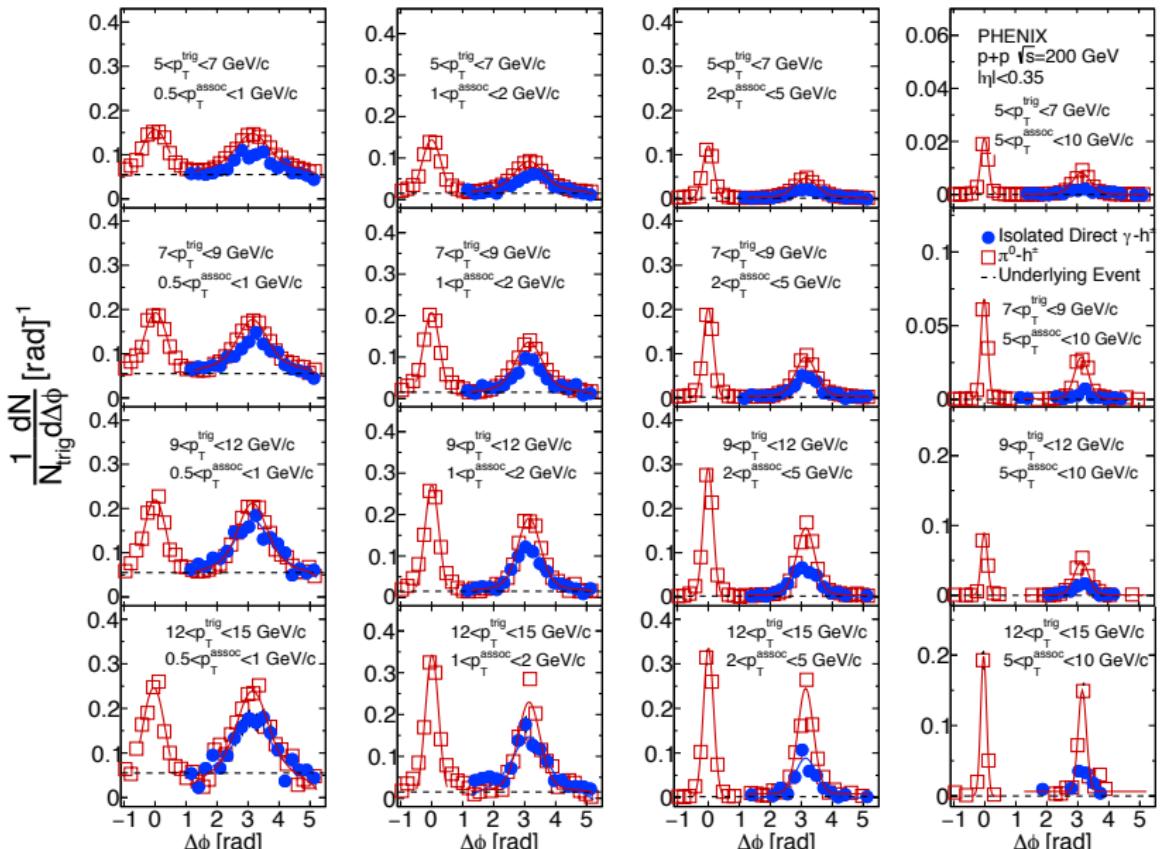
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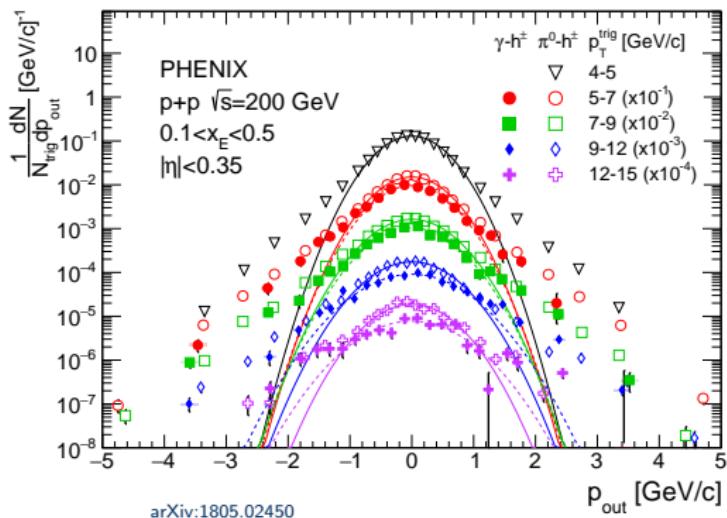
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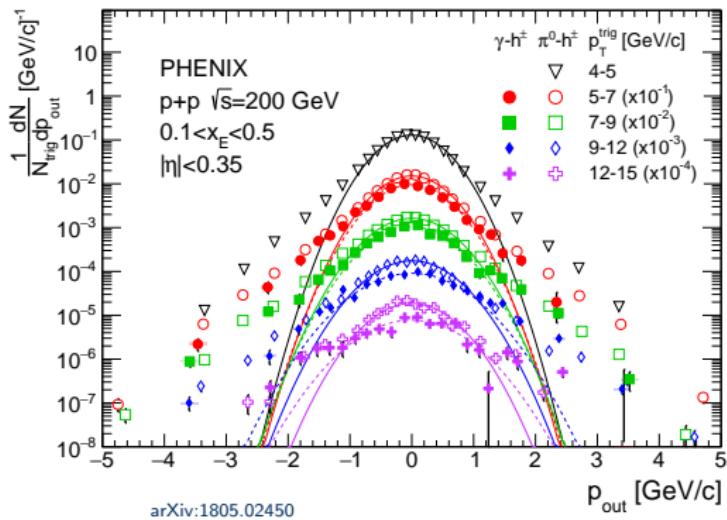
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# Measurements of $p_{\text{out}}$ Distributions in $p+p \rightarrow \text{hadrons}$

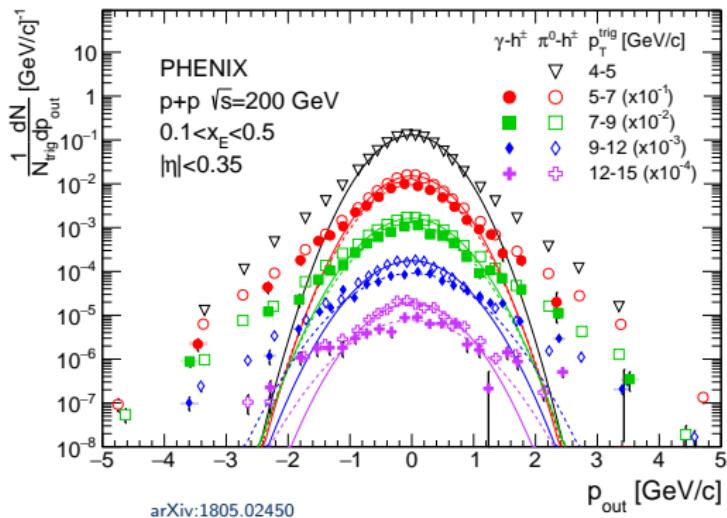


# Measurements of $p_{\text{out}}$ Distributions in $p+p \rightarrow \text{hadrons}$



- Two distinct regions:
  - Gaussian at small  $p_{\text{out}}$
  - Power law at large  $p_{\text{out}}$

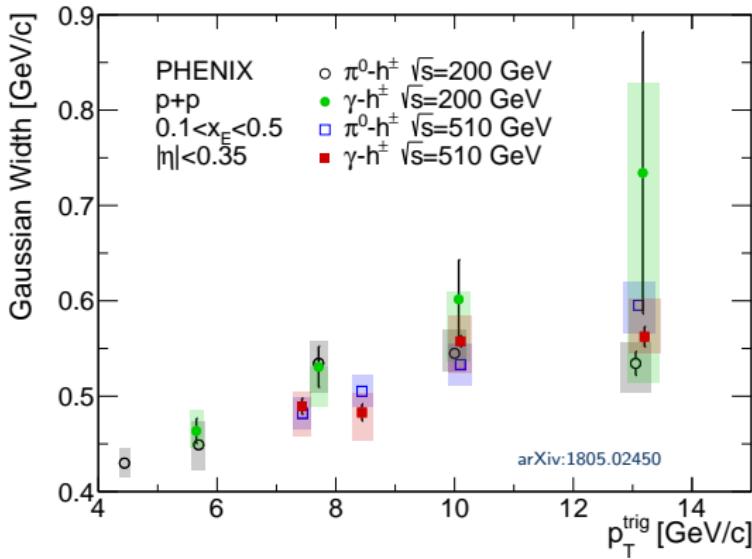
# Measurements of $p_{\text{out}}$ Distributions in $p+p \rightarrow \text{hadrons}$



- Two distinct regions:
  - Gaussian at small  $p_{\text{out}}$
  - Power law at large  $p_{\text{out}}$
- Indicates TMD observable -  
 $\Lambda_{QCD} \lesssim p_{\text{out}} \ll p_T^{\text{trig}}$
- Can characterize any potential color effects by studying width evolution as a function of  $p_T^{\text{trig}}$

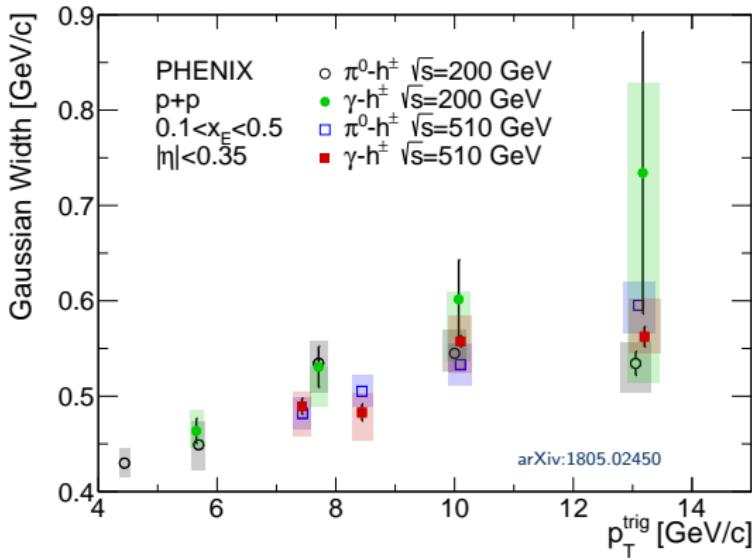
# Gaussian Width of $p_{\text{out}}$ Evolution in $p+p \rightarrow \text{hadrons}$

- Away-side Gaussian widths shown as a function of  $p_T^{\text{trig}}$  at  $\sqrt{s} = 200$  and 510 GeV

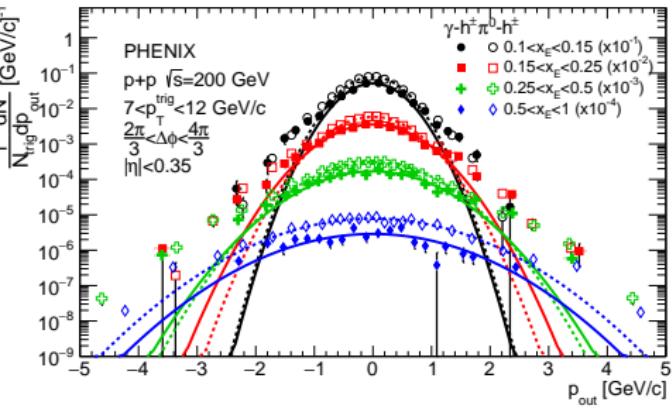
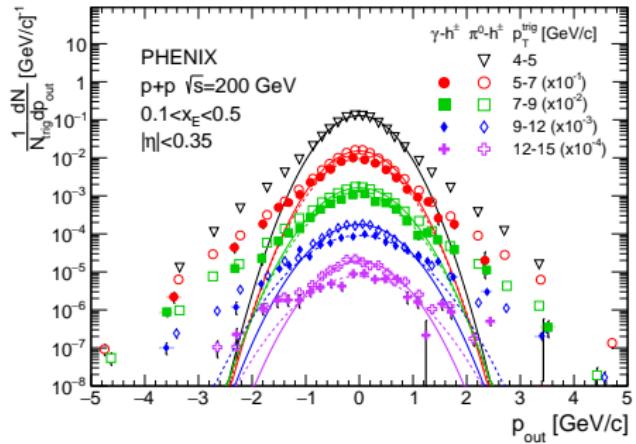


# Gaussian Width of $p_{\text{out}}$ Evolution in $p+p \rightarrow \text{hadrons}$

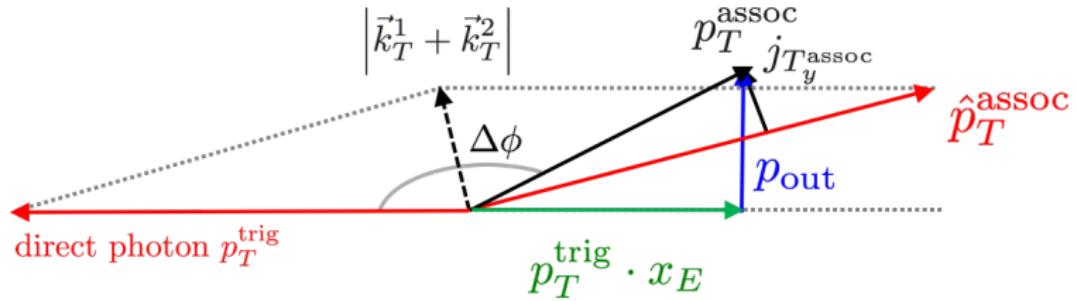
- Away-side Gaussian widths shown as a function of  $p_T^{\text{trig}}$  at  $\sqrt{s} = 200$  and 510 GeV
- Qualitatively similar behavior to Drell-Yan and semi-inclusive DIS interactions where color entanglement is not predicted



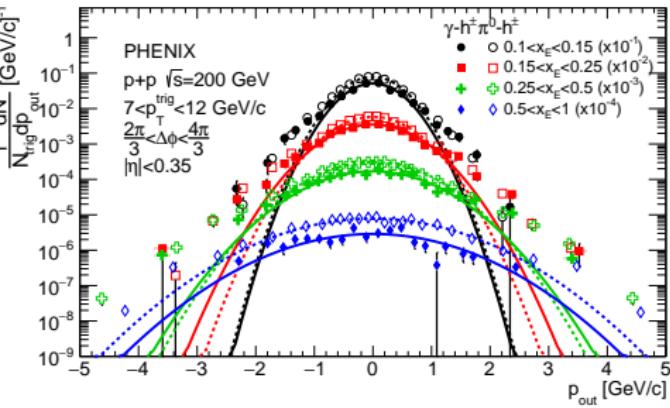
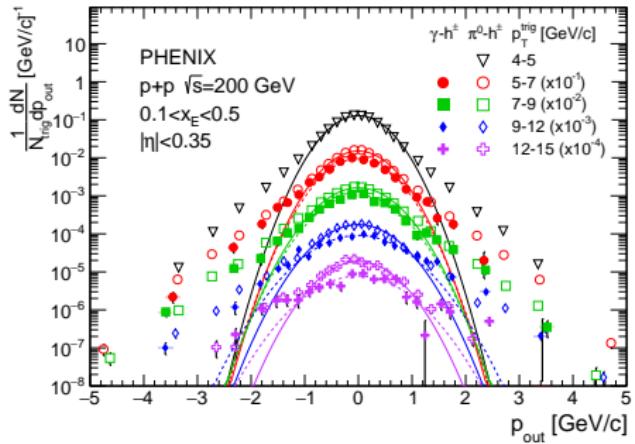
# Measurements of $p_{\text{out}}$ Distributions in $p+p \rightarrow \text{hadrons}$



arXiv:1805.02450



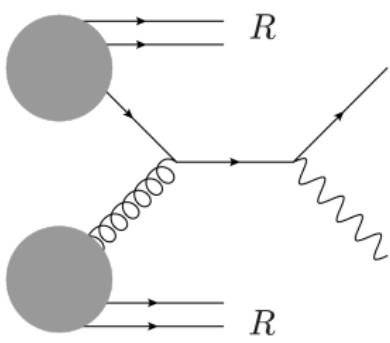
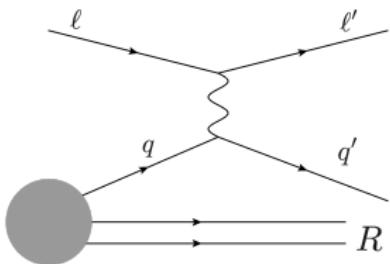
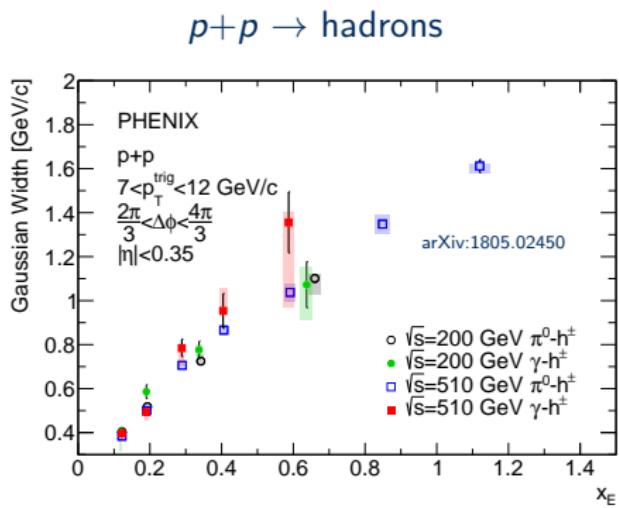
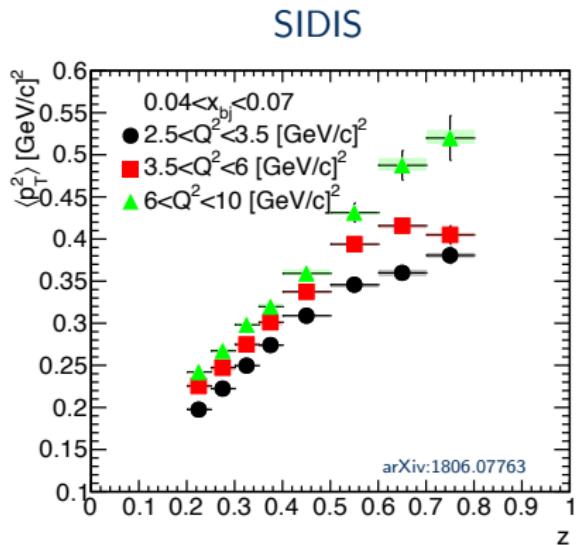
# Measurements of $p_{out}$ Distributions in $p+p \rightarrow$ hadrons



arXiv:1805.02450

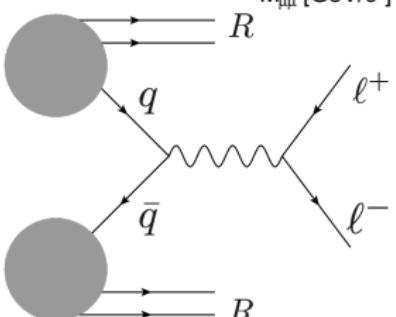
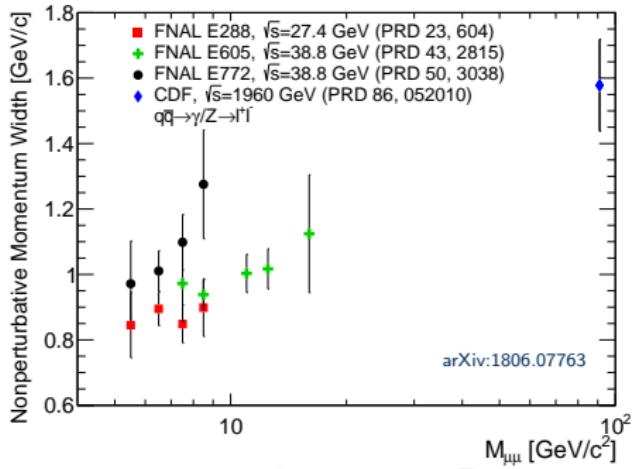
- Measure  $p_{out}$  as a function of  $p_T^{\text{trig}}$  or  $x_E$
- Multidifferential precision QCD measurements!

# Comparing SIDIS and $p+p \rightarrow$ hadrons

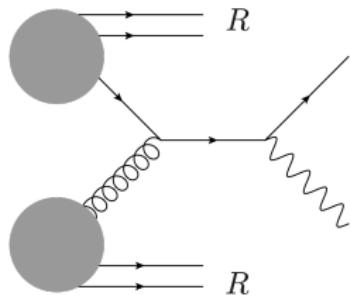
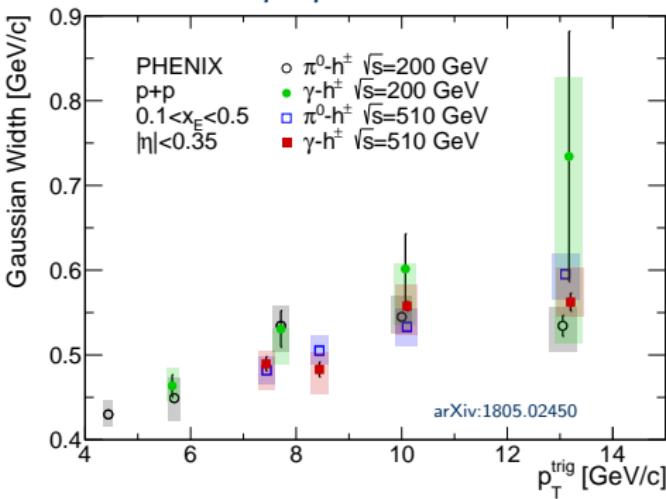


# Comparing Drell-Yan and $p+p \rightarrow$ hadrons

## Drell-Yan

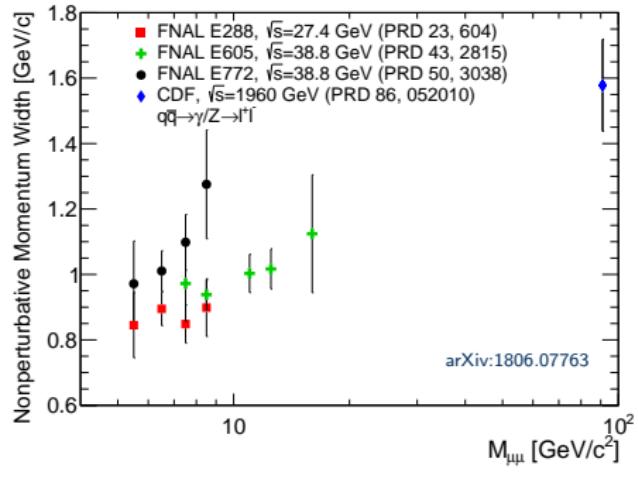


## $p+p \rightarrow$ hadrons

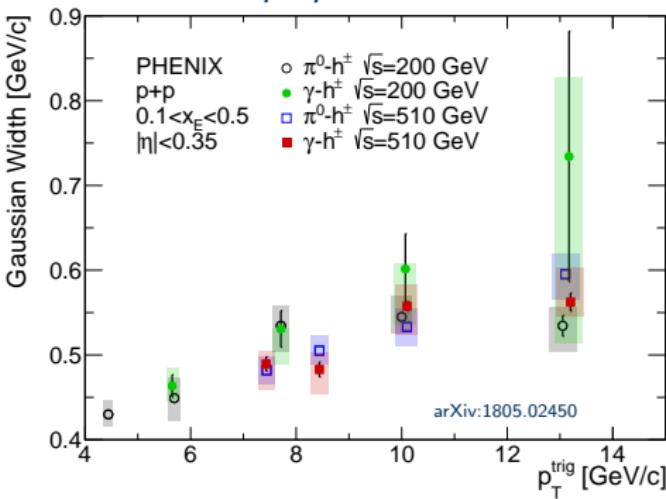


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Drell-Yan



$p+p \rightarrow$  hadrons

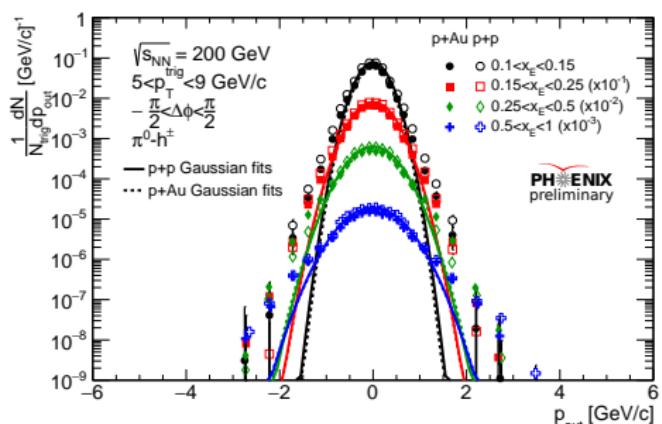


- Since qualitative behavior is similar, calculations needed to compare transverse-momentum-dependent evolution rates in different processes
- Drell-Yan/SIDIS (no color entanglement predicted) and  $p+p \rightarrow$  hadrons (color entanglement predicted) may exhibit different magnitudes, evolution rates, etc.

**What about proton-nucleus collisions, where  
there can be more QCD interactions?**

# Extending Color Studies to $p+A$

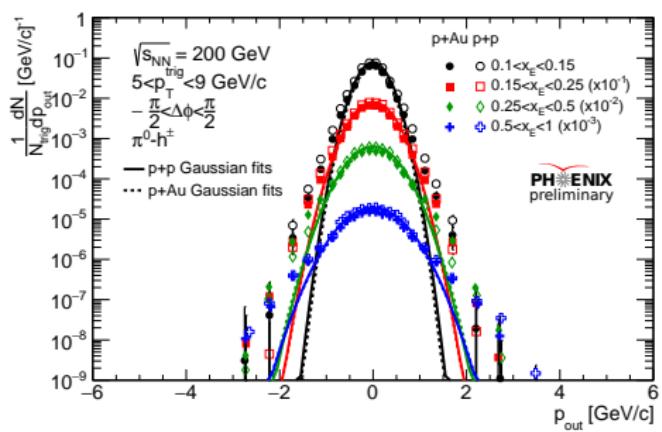
- Dihadrons give additional QCD interactions in  $p+A$  collisions compared to direct photon-hadrons
- Measure the  $p_{out}$  distributions on both the near-side and away-side in  $p+p$  and  $p+A$  to compare



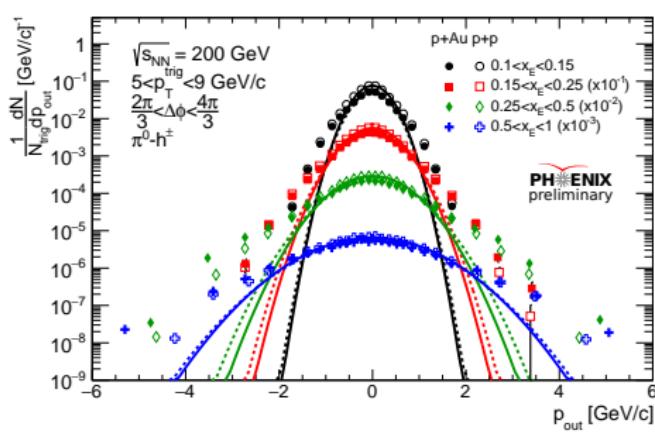
Near-side

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Near-side

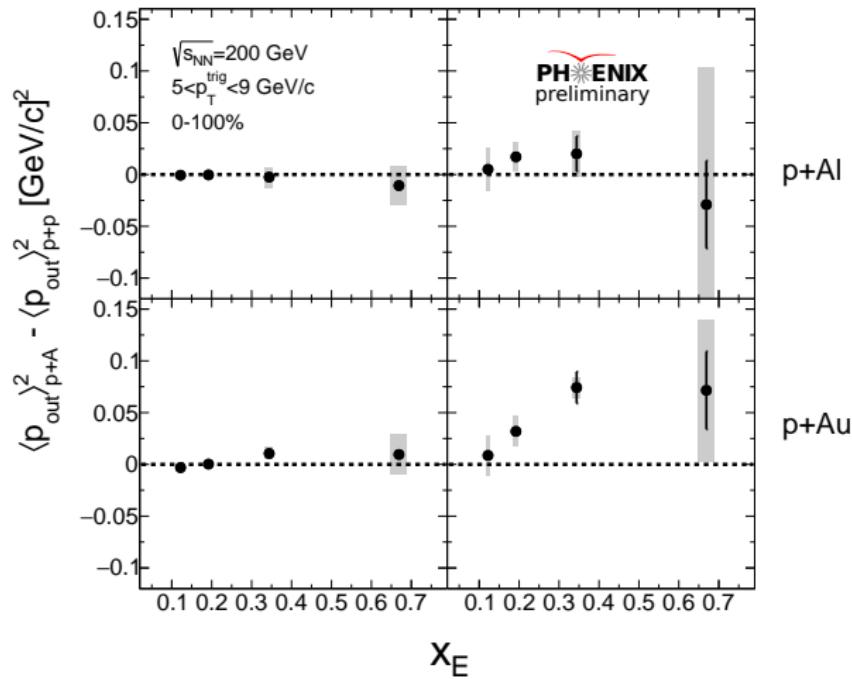


Far-side

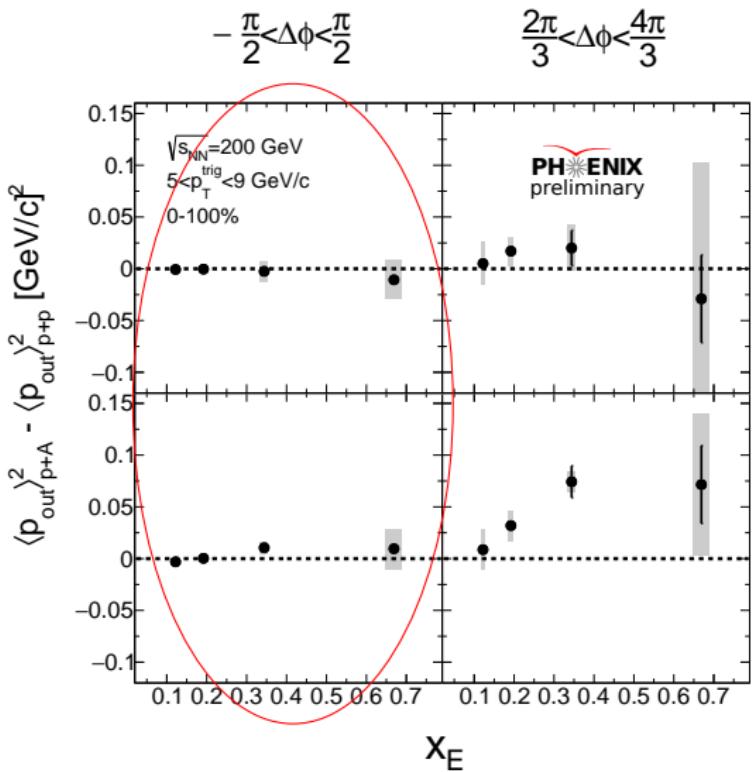
# Nonperturbative Transverse Momentum Broadening in $p+A$

$$-\frac{\pi}{2} < \Delta\phi < \frac{\pi}{2}$$

$$\frac{2\pi}{3} < \Delta\phi < \frac{4\pi}{3}$$



# Nonperturbative Transverse Momentum Broadening in $p+A$

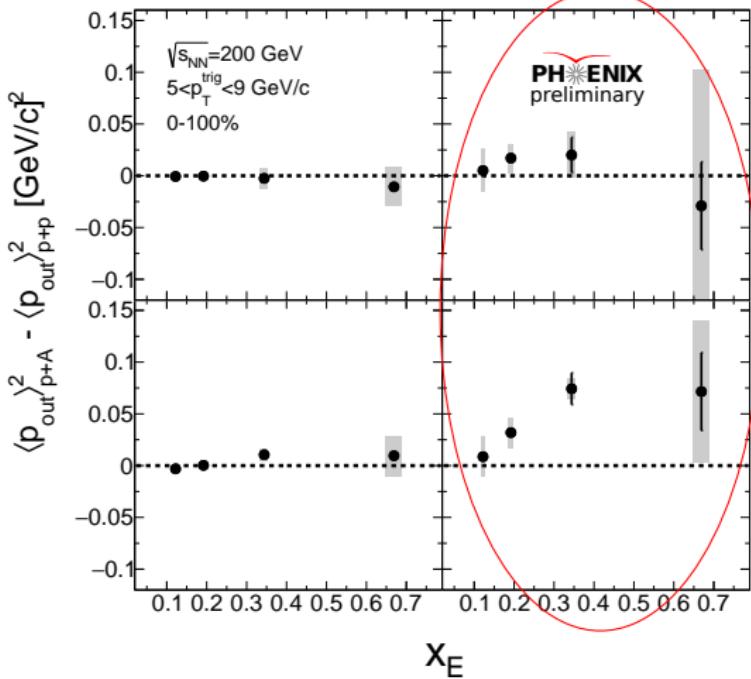


- Measure squared Gaussian width in  $p+A$  minus  $p+p$
- No significant near-side transverse momentum broadening

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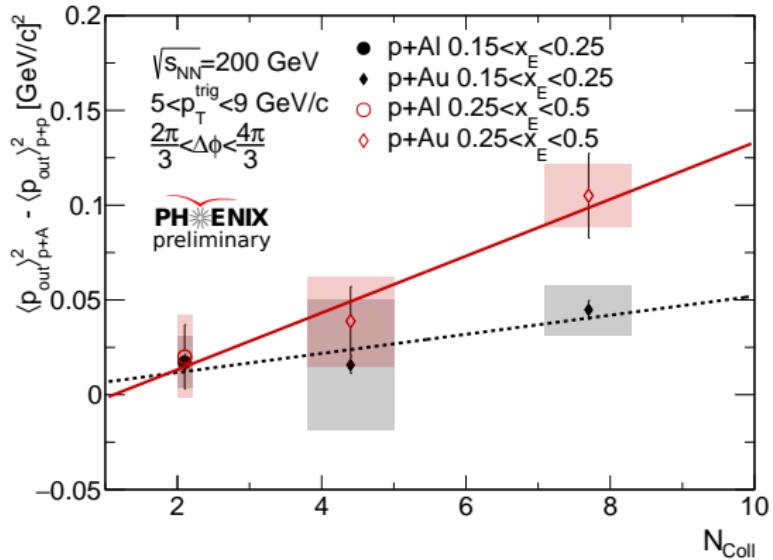


p+Al

p+Au

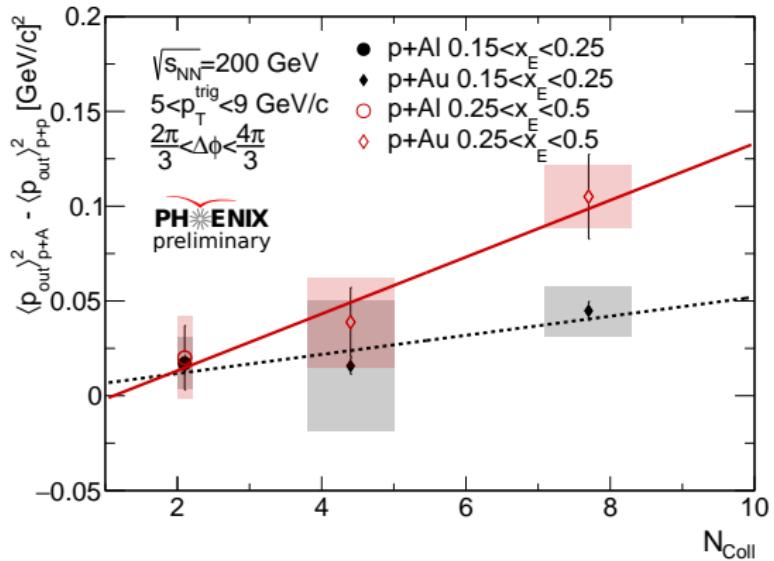
- Measure squared Gaussian width in  $p+A$  minus  $p+p$
- No significant near-side transverse momentum broadening
- Nonzero away-side nonperturbative transverse momentum broadening in  $p+A$

# Broadening as a Function of $N_{coll}$



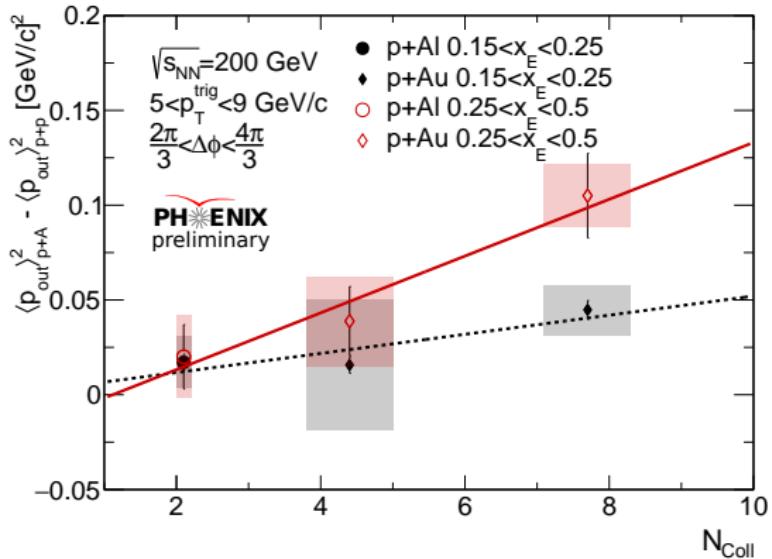
- Measure away-side transverse momentum broadening as a function of  $N_{coll} \approx$  proxy for path length

# Broadening as a Function of $N_{coll}$



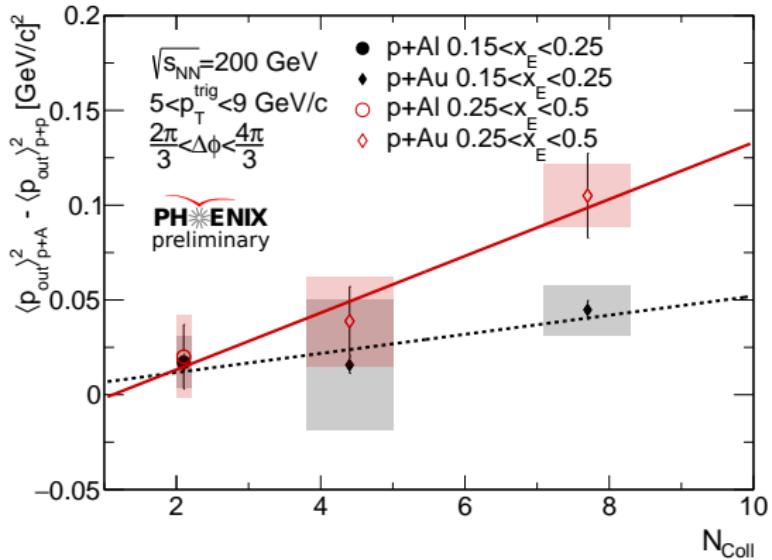
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  - Stronger color fields in nucleus?

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  - Energy loss in  $p+A$ ?
  - ...

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  - ...

- To be submitted for publication soon, stay tuned!

# Future Color Entanglement Measurements

- Color entanglement interactions require color in the initial and final states
- Crucial to make measurements at RHIC and LHC for interpreting future Electron-Ion Collider data!



# Future Color Entanglement Measurements

- Color entanglement interactions require color in the initial and final states
- Crucial to make measurements at RHIC and LHC for interpreting future Electron-Ion Collider data!
- Golden channel:  $\gamma/Z^0$ -jet → parton dynamics can be determined at leading order
- Need high  $p_T$  processes which still have sensitivity to the nonperturbative physics



## Conclusions

- Color is an integral part of QCD, but new observables and phenomenological calculations are just now exploring its consequences!

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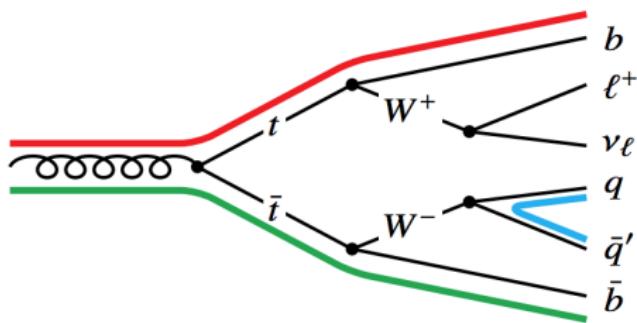
## Conclusions

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- Dihadron correlations in  $p+A$  collisions exhibit path length dependence, sensitive to color, energy loss, and more
- Future measurements at sPHENIX and LHCb will continue to probe color effects
- Synthesizing information from many different collision systems is joining historically separate fields - it's all QCD!

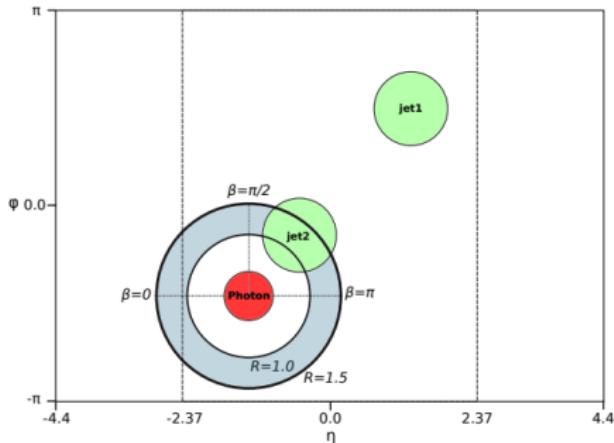
**Back up**

## $t\bar{t}$ Color Topology

- Example  $t\bar{t}$  color topology
- $t\bar{t}$  are color connected via gluon splitting
- Hadronizing quarks from  $W$  decays can also be color connected



## $\beta_\gamma$ Definition

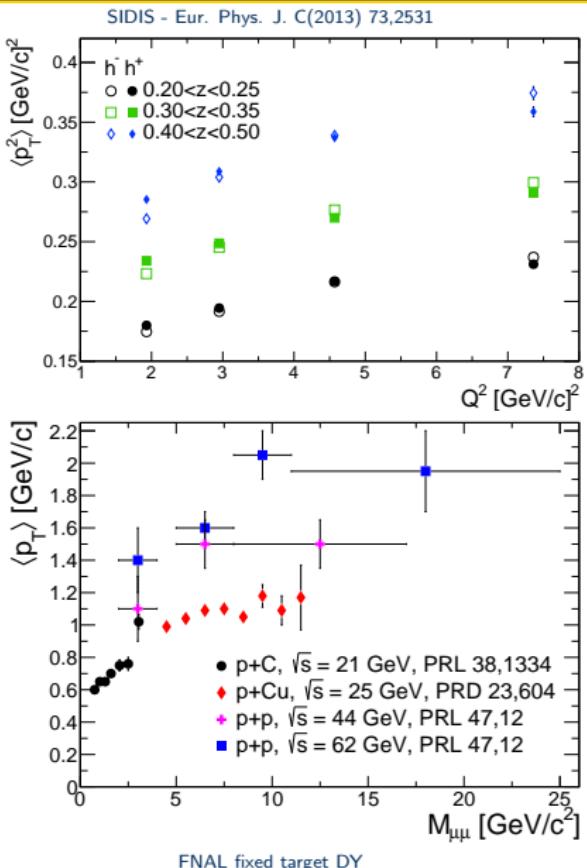


- ATLAS collaboration also measures  $\beta_\gamma$ , defined in a similar way to  $\beta_{jet}$

$$\beta^\gamma = \tan^{-1} \frac{|\phi^{jet2} - \phi^\gamma|}{\text{sign}(\eta^\gamma) \cdot (\eta^{jet2} - \eta^\gamma)}$$

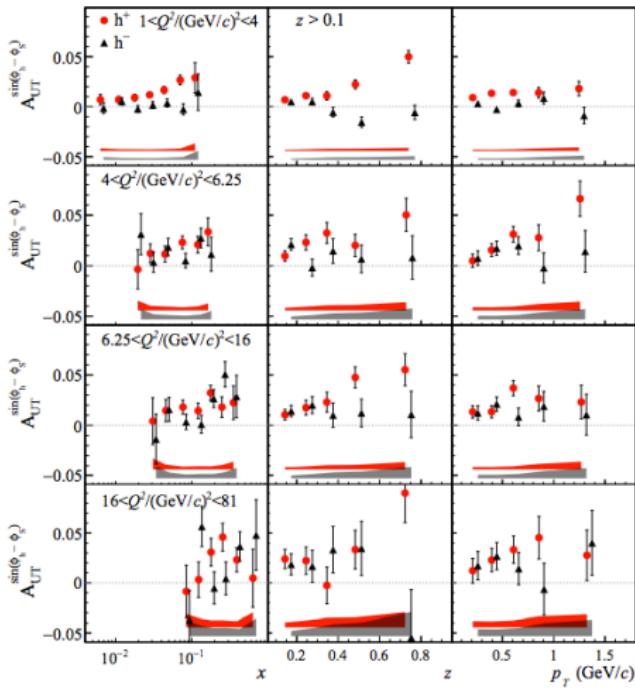
# DY/Z and SIDIS in CSS Evolution

- Measurements show that DY and SIDIS follow prediction of CSS evolution
- The CSS evolution equation comes directly out of the derivation for TMD factorization



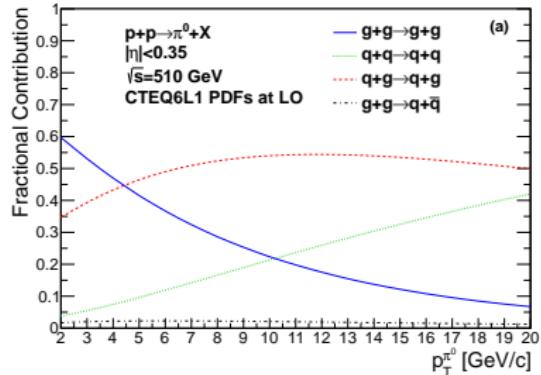
# SIDIS Sivers Measurement

- SIDIS Sivers measurement shows  $\sim 5\%$  asymmetries
- Smaller than the asymmetries measured in hadronic collisions
- SIDIS only sensitive to final-state effects from gluon exchanges

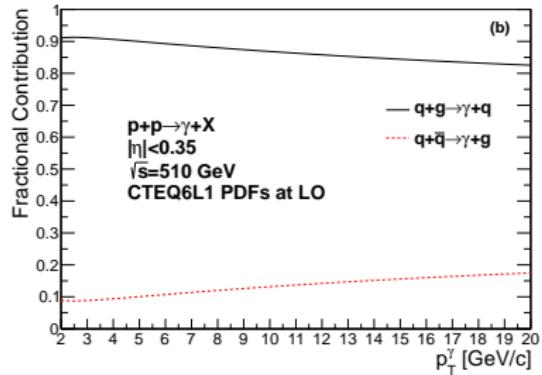


Phys. Lett. B770 (2017) 138-145

# Partonic Contributions to Processes at LO

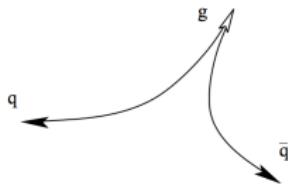


- $\pi^0$  contribution changes from gluon dominated at low  $p_T$  to mix of quark and gluons at high  $p_T$



- Direct photon contribution dominated by QCD Compton scattering at all  $p_T$
- NLO corrections small at midrapidity (Phys. Lett. B 140,87)

## More about Color Coherence



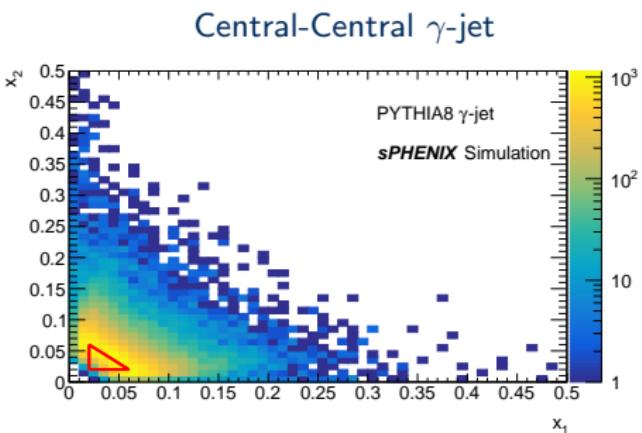
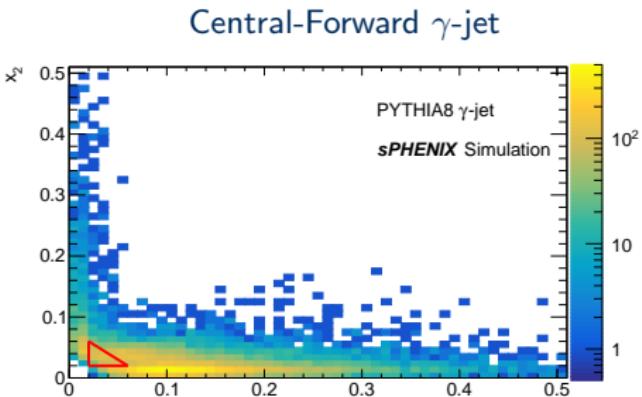
- Radiation “drags” color away from vertex
- Destructive interference occurs away from emitted gluons
- Soft radiation inhibited in certain areas
- Leads to certain regions of phase space where gluons constructively or destructively interfere

- See the following references

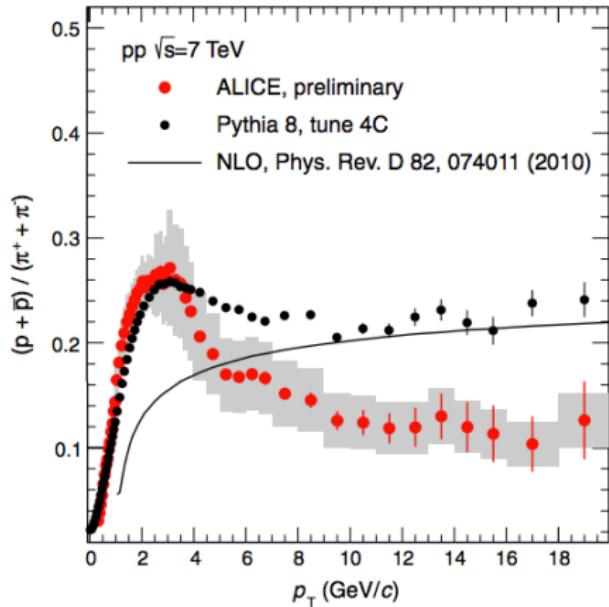
- Phys. Rev. D 50,5562 (1994)
- Phys. Lett. B 414 (1997) 419-427
- Dokshitzer, Yuri. *Basics of Perturbative QCD* (Editions Frontieres, 1991) Chapters 4,5,9

# Extending PHENIX Kinematic Reach

- Central-forward (top) and central-central (bottom)  $\gamma$ -jet  $x_1, x_2$  reach at  $\sqrt{s} = 510$  GeV. Red triangle indicates  $x_1-x_2$  reach of PHENIX PRD 95, 072002 (2017)



# Color Leads to $\nu_2$ Fourier Harmonic in PYTHIA

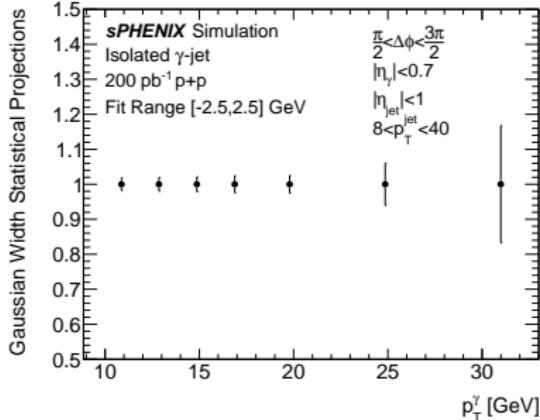
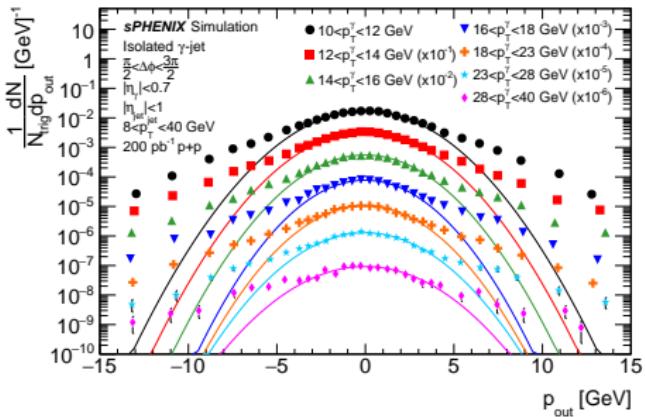


PRL 111, 042001 (2013)

- Color reconnection mechanisms within PYTHIA exhibit similar characteristics to measured Fourier harmonics in  $p+p$
- Can color coherence generate long range eta correlations and PID radial flow patterns?
- Multiple partonic interactions are necessarily color connected

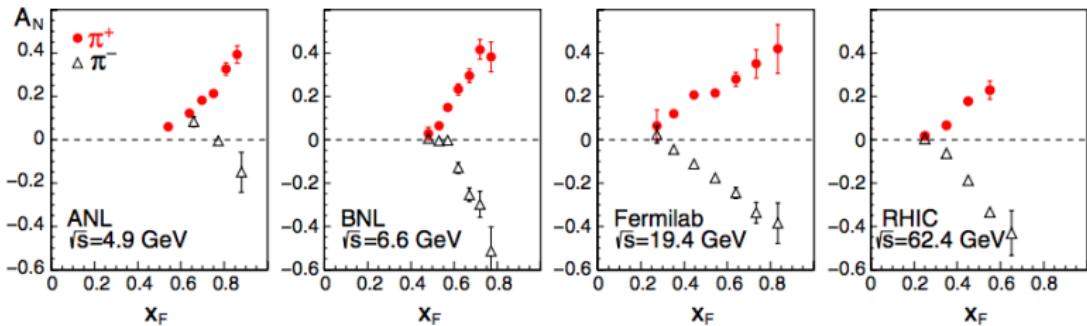
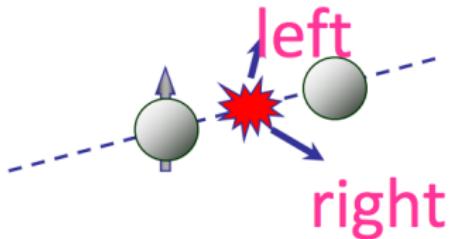
# Estimated $\gamma$ -jet Statistical Precision

- $\gamma$ -jet is the ideal channel - limits color flow possibilities with sensitivity to only  $k_T$
- RHIC kinematics important - need high  $p_T$  processes which still have sensitivity to the nonperturbative physics
- sPHENIX will have excellent statistical precision for  $\gamma$ -jet at RHIC *for the first time*
- Will extend PRD 95, 072002 (2017) to study  $x$  dependence as well as role of fragmentation with tracking capabilities



# Relation to Huge Transverse Single Spin Asymmetries?

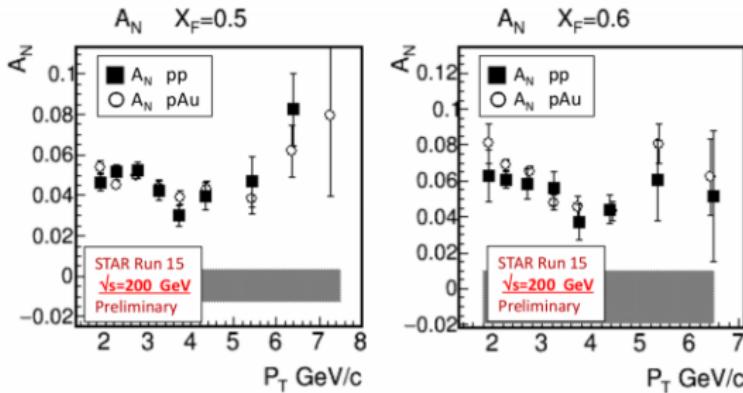
- Transverse single spin asymmetries show up to 40% left-right asymmetry in  $p+p$  collisions
- Only  $\sim 5\%$  in semi-inclusive DIS
- Effects from color contributing?



Rev. Mod. Phys. 85, 655 (2013)

# Relation to Huge Transverse Single Spin Asymmetries?

- Transverse single spin asymmetries are perturbatively predicted to go to 0 with increasing  $p_T$
- Nonzero ( $\sim 7\%$ ) asymmetries have been measured up to  $p_T \sim 7$  GeV
- Transverse single spin asymmetries seem to not follow perturbative evolution as well
- Do correlations follow expectation of magnitudes for perturbative evolution? Calculations necessary...



# Transverse-Momentum-Dependent PDF Zoo

## Transverse-Momentum-Dependent (TMD) PDFs

N q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1$ $h_{1T}^\perp$

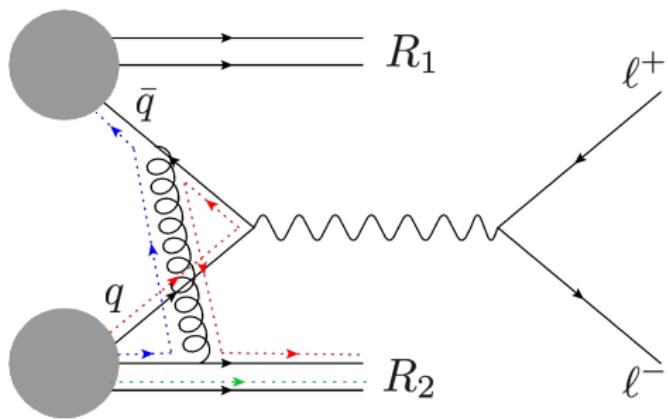
N - Nucleon  
q - Quark  
U - Unpolarized  
L - Longitudinally polarized  
T - Transversely polarized

Image taken from Alexei Prokudin Spin 2016

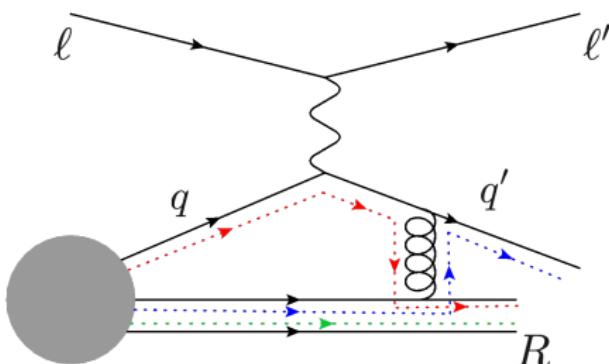
- 8 TMD PDFs describing transverse partonic structure, spin-spin, and spin-momentum *correlations!*

# Universality in Transverse-Momentum-Dependent Functions

Drell-Yan:  $q + \bar{q} \rightarrow \ell^+ + \ell^-$



Semi-Inclusive DIS:  $e^- + p \rightarrow e^- + h$

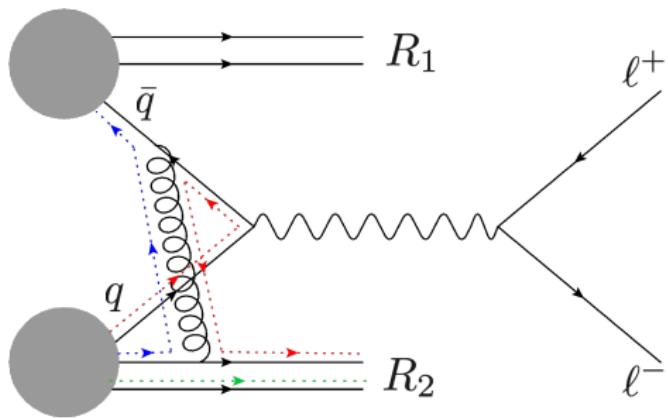


- Sign change in parity-time odd transverse-momentum-dependent PDFs predicted due to initial-state vs. final-state gluon exchange with proton remnants in different processes!

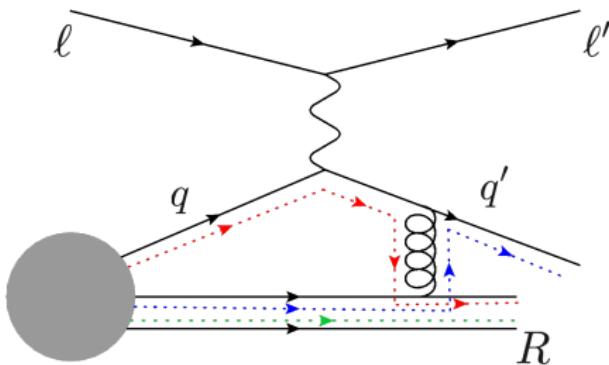
$$f_{1T}^\perp(x, k_T, Q^2)|_{\text{DY}} = -f_{1T}^\perp(x, k_T, Q^2)|_{\text{SIDIS}}$$

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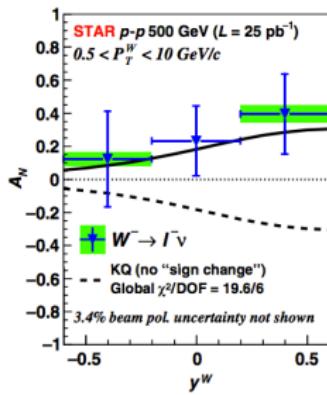
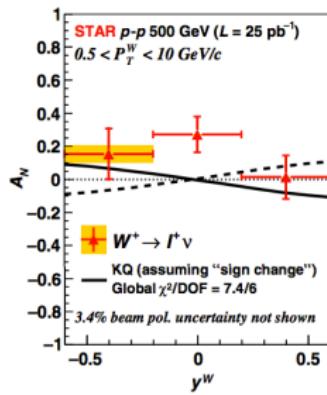
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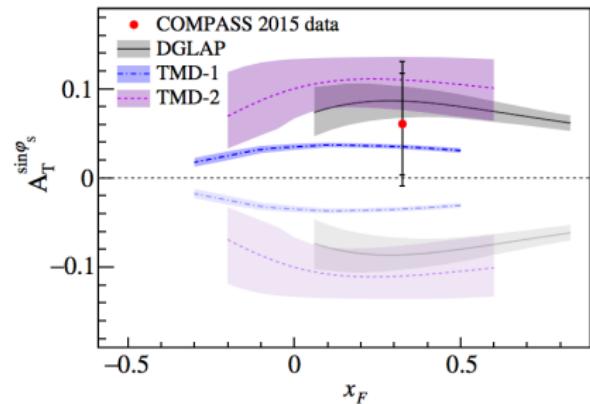
- Sign change in parity-time odd transverse-momentum-dependent PDFs predicted due to initial-state vs. final-state gluon exchange with proton remnants in different processes!
- Factorization of transverse-momentum-dependent PDFs and fragmentation functions still predicted to hold in these QED processes

# First Measurement of Possible Modified Universality

- Semi-inclusive DIS Sivers asymmetries have been measured, e.g. by HERMES and COMPASS collaborations
- First measurements of Drell-Yan (type) processes just recently reported
- Data support prediction of process dependent transverse-momentum-dependent PDF (although still statistically limited)



PRL 116, 132301(2016)



PRL 119, 112002 (2017)